

# COMPUTER NUMERICAL CONTROL OF MACHINE TOOLS

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Patras 2016

# Chapter 7: Tolerancing

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# Objectives

- Learn about **tolerancing** and how important this technique is, to mass production
- Learn various **tolerancing methods**
- Learn about **tolerancing standards** and the most common standards agencies
- And, ways of formatting **inch and metric tolerances**



# Introduction

- After completing the construction of a piece, its **dimensions appear to deviate** compared to its nominal values
- These variations depend on the **accuracy of the machine-tools** used and the **available measuring devices**
- **Minor deviations**, depending on the intended use of the piece, **may be tolerated without destroying its functionality**
- **Tolerances** are defined as the **permissible deviations** from the prescribed shape, size or position of an element in one piece **with respect to the corresponding ones of the drawing**

(Φυλλάδιο εργαστηριακών ασκήσεων Μηχανουργείου, 2012, Μούρτζης Δ. κ.α.)

# Tolerances

- In most of the cases the craftsman who undertakes the construction of a piece is **unable to reproduce the exact dimensions** as outlined in the drawing
- For this reason **constructional drawings indicate the permissible deviations** from the nominal dimension
  - Example:

A given dimension in a drawing is  **$1.50 \pm .04$  mm**, meaning that the piece **should have a particular dimension between 1.46 and 1.54 mm**, and that the **possible permissible tolerance** on this dimension is **0.08 mm**

(Φυλλάδιο εργαστηριακών ασκήσεων Μηχανουργείου,2012, Μούρτζης Δ. κ.α.)

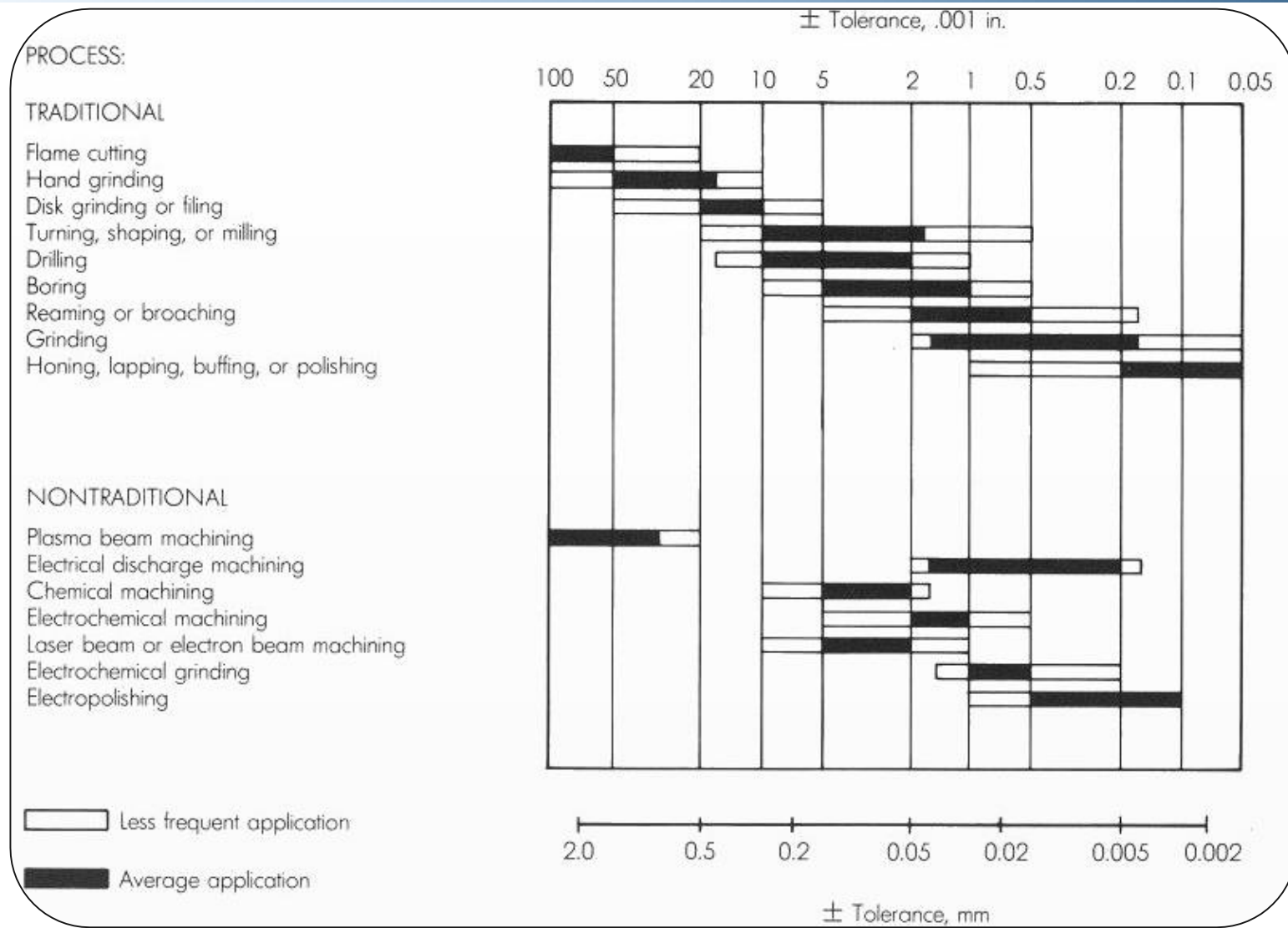
# Tolerances



## Greater accuracy requires greater cost

- For this reason **not all the parts of a product are constructed with the same accuracy** (same tolerances)
- The selection of the desired **accuracy** of a product's part **depends on its final use** (assembly with other parts, e.g., shaft and hole, etc.).
- **Tolerances** are **heavily dependent on the machine tool** used for the manufacturing of the piece
- The following figure presents the typical achievable tolerances for various production material removal processes

# Tolerances

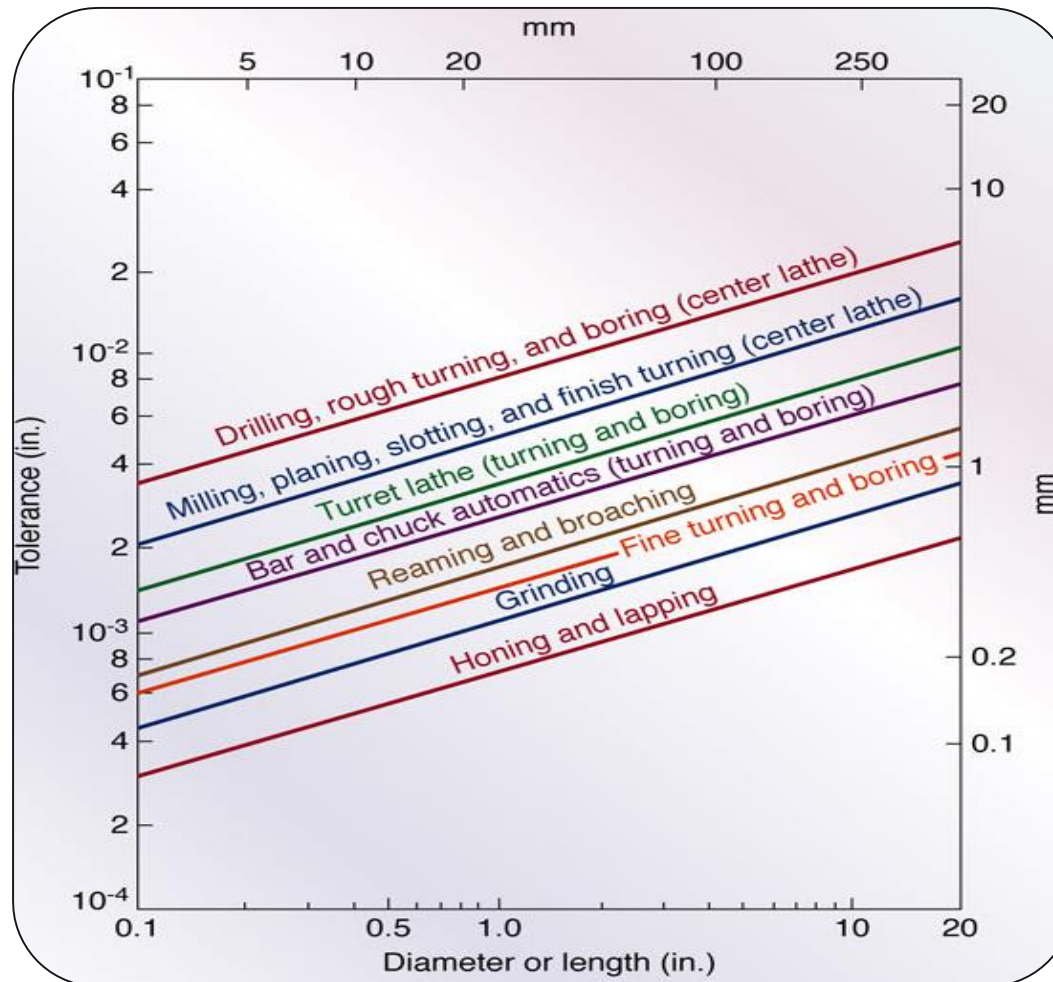


**Figure 1: Typical tolerances for material removal processes**

(Φυλλάδιο εργαστηριακών ασκήσεων Μηχανουργείου ,Μούρτζης Δ. κ.α. , Πανεπιστήμιο Πατρών)



# Tolerances



**Figure 2: Range of Dimensional Tolerances in Machining as a Function of Workpiece Size**

(source: Manufacturing, Engineering & Technology, Fifth Edition, by S. Kalpakjian and Steven R. Schmid )

# I. Tolerancing for Interchangeability

# Tolerancing / Interchangeability

- **Tolerancing is dimensioning for interchangeability**  
An interchangeable part is simply a mass produced part  
(a replacement part)
- **Tolerancing** allows a **range specification of accuracy** for every feature of a product, so the parts will fit together and function properly when assembled
- How is a feature on an interchangeable part dimensioned?
  - The feature is **not dimensioned using a single value**, but a **range** of values

1.00 → 1.005  
.994

# Tolerancing / Interchangeability

- **Tolerance** is the **total amount a specific dimension is permitted to vary**
- Usage of **generous tolerances** when possible is preferred because increased precision makes parts more **expensive to manufacture**
- A tolerance that specifies a large or small variation can be chosen

# Understanding Tolerance

**Size limits :**      1.005  
                              .994

**Tolerance :**  $1.005 - .994 = .011$

# Tolerancing / Interchangeability

- Why do we want a part's size to be controlled by two limits?
- It is necessary because it is **impossible to manufacture parts without some variation**
- The stated limits are a form of quality control

# Tolerancing / Interchangeability

- Choosing the correct tolerance for a particular application depends on:

 **the design intent** (end use) of the part

 **cost**

 **how it is manufactured**

 **experience**

## II. Tolerance Types



# Tolerance Types

- The tolerancing methods presented are:
  - 1. Limit dimensions**
  - 2. Plus or minus tolerances**
  - 3. Page or block tolerances**

# 1. Limit Dimensions

- **Limits** are the **maximum and minimum size** that a part can obtain and still pass inspection
  - For example, the diameter of a shaft might be specified as follows.

$\varnothing \begin{matrix} 1.001 \\ .999 \end{matrix}$  or  $\varnothing 1.001 - .999$

# 1. Limit Dimension Order

- **External dimensions:**

- The larger dimension is first or on top and the smaller dimension is last or on the bottom

- **Internal dimensions:**

- The smaller dimension is first and the larger dimension is last

## 2. Plus or Minus Tolerances

- **Plus or minus tolerances** give a basic size and the variation that can occur around that basic size

$$10.0 \begin{matrix} +0.1 \\ -0.2 \end{matrix}$$

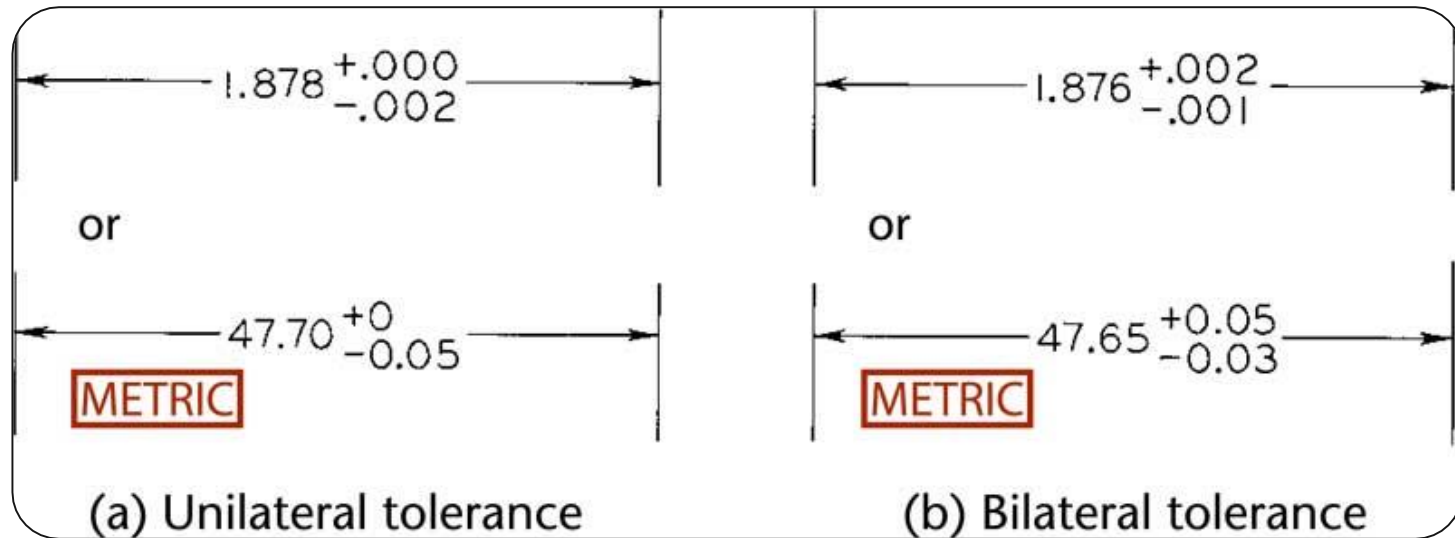


Figure 3: Example of plus or minus tolerances

# 3. Page or Block Tolerances

- A **page tolerance** is actually a general note that applies to all dimensions not covered by some other tolerancing type

UNLESS OTHERWISE SPECIFIED ALL:

.XX =  $\pm$  .010 inch

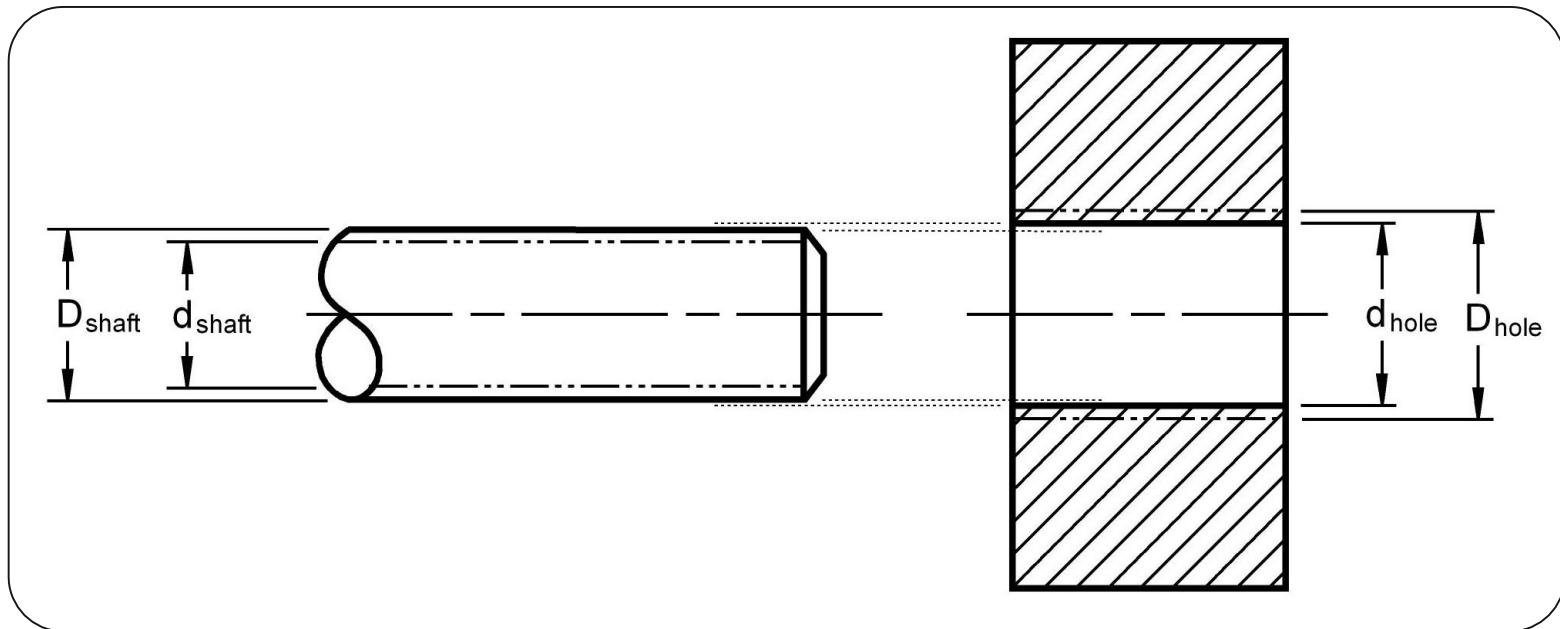
.XXX =  $\pm$  .005 inch

.XXXX =  $\pm$  .002 inch

# III. General Definitions

# General Definitions

- What are the **limits**, **tolerance** and **allowance** for the following shaft/hole system? Are they the same or different?



# General Definitions

- **Limits**

Are the **maximum** and **minimum diameters**

- **Tolerance**

Is the **difference between two limits**

- **Allowance** (Minimum Clearance)

Is the **difference** between the **largest shaft diameter** and the **smallest hole diameter**

*(K. Plantenberg , 2006, )*

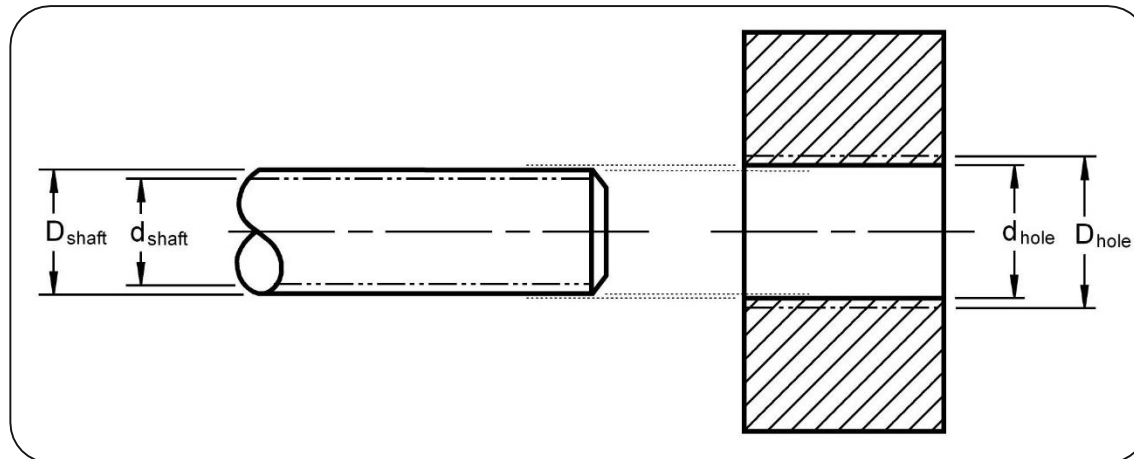


# Example 1

- What are the **limits** of the shaft and the hole?

➤ Shaft:  $D_{\text{shaft}} - d_{\text{shaft}}$

➤ Hole:  $d_{\text{hole}} - D_{\text{hole}}$

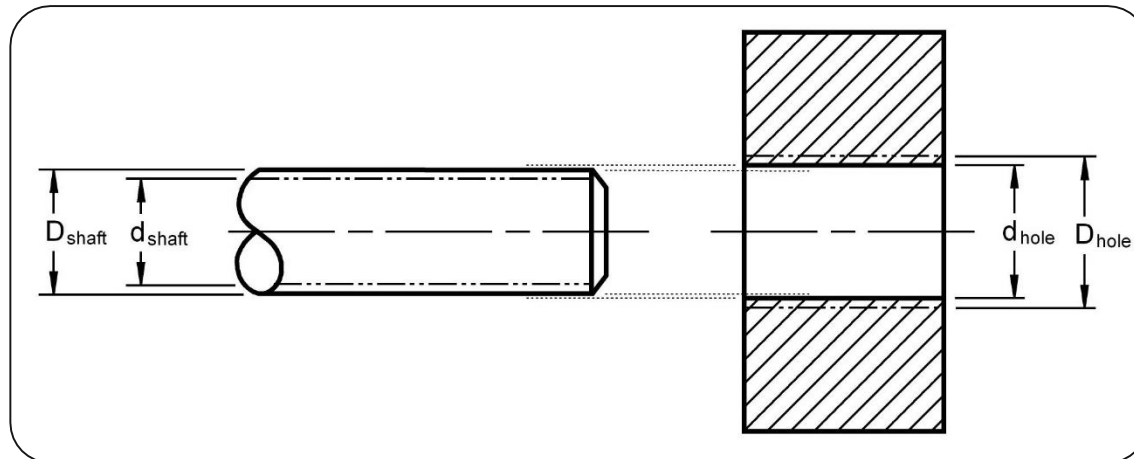


# Example 2

- What is the **tolerance** for the shaft and the hole?

➤ Shaft:  $D_{\text{shaft}} - d_{\text{shaft}} = \dots$

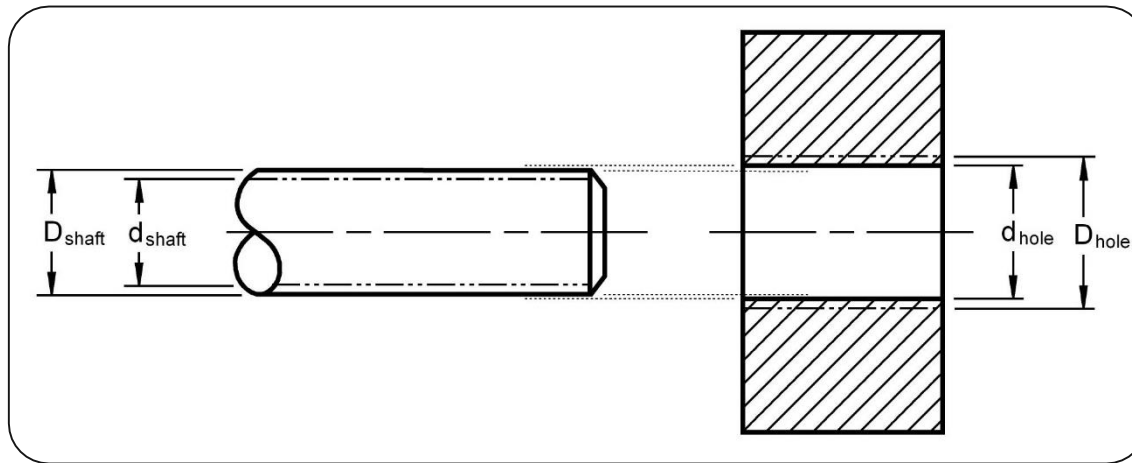
➤ Hole:  $D_{\text{hole}} - d_{\text{hole}} = \dots$



# Example 3

- What is the **minimum clearance** (allowance)?

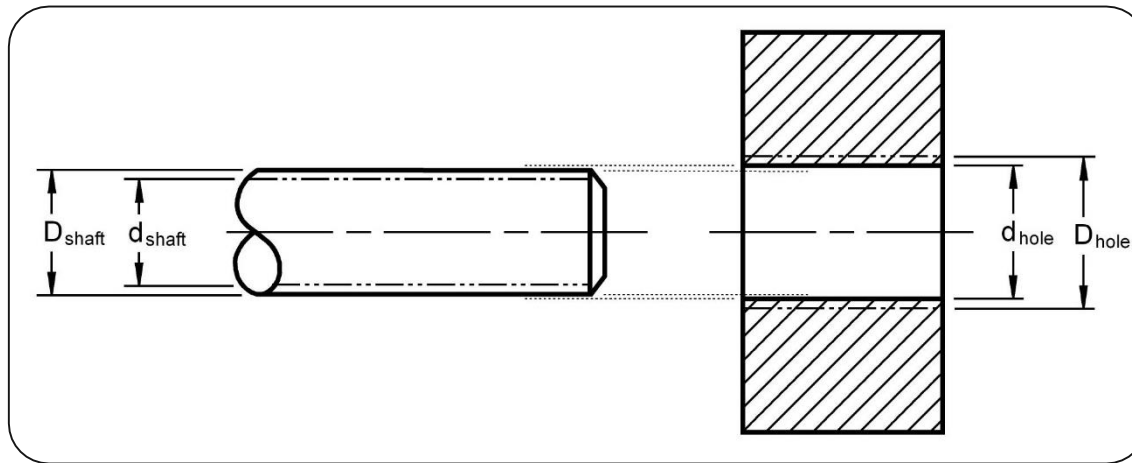
$$d_{\text{hole}} - D_{\text{shaft}} =$$



# Example 4

- What is the **maximum clearance**?

$$D_{\text{hole}} - d_{\text{shaft}} =$$



# IV. Tolerancing Standards

# Tolerancing Standards

- **Standards** are needed to:

 Make it possible to manufacture parts at **different times** and in **different places** that still **assemble properly**

 Establish **dimensional limits** for parts that are to be **interchangeable**

# Tolerancing Standards

- **The two most common standards agencies are;**
  - **American National Standards Institute (ANSI) / (ASME)**
  - **International Standards Organization (ISO)**

# V. Inch Tolerances



# Inch Tolerances Definitions

- **Limits**

The limits are the **maximum** and **minimum size** that the part is allowed to be

- **Basic Size**

The **basic size** is the size from which the **limits are calculated**

- It is common for both the hole and the shaft and is usually the closest fraction

- **Tolerance**

The **tolerance** is the total amount a **specific dimension is permitted to vary**

*(K. Plantenberg , 2006, )*

# Inch Tolerances Definitions

- **Maximum Material Condition (MMC):**

The MMC is the size of the part when it consists of the most material

- **Least Material Condition (LMC):**

The LMC is the size of the part when it consists of the least material

# Inch Tolerances Definitions

- **Maximum Clearance:**

The maximum amount of space that can exist between the hole and the shaft

$$\text{Max. Clearance} = \text{LMC}_{\text{hole}} - \text{LMC}_{\text{shaft}}$$

- **Minimum Clearance (Allowance):**

The minimum amount of space that can exist between the hole and the shaft

$$\text{Min. Clearance} = \text{MMC}_{\text{hole}} - \text{MMC}_{\text{shaft}}$$

# Types of Fits

- **Clearance Fit** : There is always a space, **Min. Clearance  $> 0$**
- **Interference Fit** : There is never a space, **Max. Clearance  $\leq 0$**
- **Transition Fit** : Depending on the sizes of the shaft and hole there could be a space or no space, **Max. Clearance  $> 0$**   
**Min. Clearance  $< 0$**
- **Line Fit** : There is a space or a contact (hole diameter = shaft diameter), **Max. Clearance  $> 0$**   
**Min. Clearance = 0**

(K. Plantenberg , 2006, )

# Types of Fits

- From everyday life, list some examples of clearance and interference fits

## Fit

## Example

Clearance

Lock and Key

Door and Door frame

Coin and Coin slot

Interference

Pin in a bicycle chain

Hinge pin

Wooden peg and hammer toy

# Example 5

- Determine the basic size and type of fit given the limits for the shaft and hole

## Shaft Limits

## Hole Limits

1.500 – 1.498

1.503 – 1.505

1.5

Clearance

.755 - .751

.747 - .750

.75

Interference

.378 - .373

.371 - .375

.375

Transition

.250 - .247

.250 - .255

.25

Line

# ANSI Standard Limits and Fits

The following fit types and classes are in accordance with the **ANSI B4.1-1967(R1994)** standard

- **RC: Running or Sliding Clearance fit**
  - Intended to provide running performance with suitable lubrication.
  - RC9 (loosest) – RC1 (tightest)
- **FN: Force Fits**
  - Force fits provide a constant bore pressure throughout the range of sizes.
  - FN1 – FN5 (tightest)

# ANSI Standard Limits and Fits

- **Locational fits (LC, LT, LN)**

➤ **Locational fits** are intended to determine only the **location of the mating parts**

**LC** = Locational clearance fits

**LT** = Locational transition fits

**LN** = Locational interference fits



# Example 6

- Given a basic size of .50 inches and a fit of RC8, calculate the limits for both the hole and the shaft
  - Use the **ANSI limits and fit tables** given in the following Appendix

# Appendix

| Nominal Size Range Inches |         | Class RC5       |               | Class RC6       |               | Class RC7       |                | Class RC8       |                | Class RC9       |                |
|---------------------------|---------|-----------------|---------------|-----------------|---------------|-----------------|----------------|-----------------|----------------|-----------------|----------------|
|                           |         | Standard Limits |               | Standard Limits |               | Standard Limits |                | Standard Limits |                | Standard Limits |                |
| Over                      | To      | Hole            | Shaft         | Hole            | Shaft         | Hole            | Shaft          | Hole            | Shaft          | Hole            | Shaft          |
| 0                         | - 0.12  | +0.6<br>0       | -0.6<br>-1.0  | +1.0<br>0       | -0.6<br>-1.0  | +1.0<br>0       | -1.0<br>-1.6   | +1.6<br>0       | -2.5<br>-3.5   | +2.5<br>0       | -4.0<br>-5.6   |
| 0.12                      | - 0.24  | +0.7<br>0       | -0.8<br>-1.3  | +1.0<br>0       | -0.6<br>-1.0  | +1.0<br>0       | -1.2<br>-1.9   | +1.8<br>0       | -2.8<br>-4.0   | +3.0<br>0       | -4.5<br>-6.0   |
| 0.24                      | - 0.40  | +0.9<br>0       | -1.0<br>-1.6  | +1.0<br>0       | -0.6<br>-1.0  | +1.0<br>0       | -1.6<br>-2.5   | +2.2<br>0       | -3.0<br>-4.4   | +3.5<br>0       | -5.0<br>-7.2   |
| 0.40                      | - 0.71  | +1.0<br>0       | -1.2<br>-1.9  | 0               | -2.2          | 0               | -3.0           | +2.8<br>0       | -3.5<br>-5.1   | +4.0<br>0       | -6.0<br>-8.8   |
| 0.71                      | - 1.19  | +1.2<br>0       | -1.6<br>-2.4  | +2.0<br>0       | -1.6<br>-2.8  | +2.0<br>0       | -2.5<br>-3.7   | +3.5<br>0       | -4.5<br>-6.5   | +5.0<br>0       | -7.0<br>-10.5  |
| 1.19                      | - 1.97  | +1.6<br>0       | -2.0<br>-3.0  | +2.5<br>0       | -2.0<br>-3.6  | +2.5<br>0       | -3.0<br>-4.6   | +4.0<br>0       | -5.0<br>-7.5   | +6.0<br>0       | -8.0<br>12.0   |
| 1.97                      | - 3.15  | +1.8<br>0       | -2.5<br>-3.7  | +3.0<br>0       | -2.5<br>-4.3  | +3.0<br>0       | -4.0<br>-5.8   | +4.5<br>0       | -6.0<br>-9.0   | +7.0<br>0       | -9.0<br>-13.5  |
| 3.15                      | - 4.73  | +2.2<br>0       | -3.0<br>-4.4  | +3.5<br>0       | -3.0<br>-5.2  | +3.5<br>0       | -5.0<br>-7.2   | +5.0<br>0       | -7.0<br>-10.5  | +9.0<br>0       | -10.0<br>-15.0 |
| 4.73                      | - 7.09  | +2.5<br>0       | -3.5<br>-5.1  | +4.0<br>0       | -3.5<br>-6.0  | +4.0<br>0       | -6.0<br>-8.5   | +6.0<br>0       | -8.0<br>-12.0  | +10.0<br>0      | -12.0<br>-18.0 |
| 7.09                      | - 9.85  | +2.8<br>0       | -4.0<br>-5.8  | +4.5<br>0       | -4.0<br>-6.8  | +4.5<br>0       | -7.0<br>-9.8   | +7.0<br>0       | -10.0<br>-14.5 | +12.0<br>0      | -15.0<br>-22.0 |
| 9.85                      | - 12.41 | +3.0<br>0       | -5.0<br>-7.0  | +5.0<br>0       | -5.0<br>-8.0  | +5.0<br>0       | -8.0<br>-11.0  | +8.0<br>0       | -12.0<br>-17.0 | +12.0<br>0      | -18.0<br>-26.0 |
| 12.41                     | - 15.75 | +3.5<br>0       | -6.0<br>-8.2  | +6.0<br>0       | -6.0<br>-9.5  | +6.0<br>0       | -10.0<br>-13.5 | +9.0<br>0       | -14.0<br>-20.0 | +14.0<br>0      | -22.0<br>-31.0 |
| 15.75                     | - 19.69 | +4.0<br>0       | -8.0<br>-10.5 | +6.0<br>0       | -8.0<br>-12.0 | +6.0<br>0       | -12.0<br>-16.0 | +10.0<br>0      | -16.0<br>-22.0 | +16.0<br>0      | -25.0<br>-35.0 |

Basic size = .5  
Fit = RC8

# Example 7

- Given a basic size of .50 inches and a fit of RC8, calculate the limits for both the hole and the shaft.
  - Standard Limits Hole = +2.8    0
  - Standard Limits Shaft = -3.5    -5.1
- These are the values that we add/subtract from the basic size to obtain the limits

# Example 8

- Given a basic size of .50 inches and a fit of RC8, calculate the limits for both the hole and the shaft.

➤ Hole Limits =  $.50 - 0 = .5000$

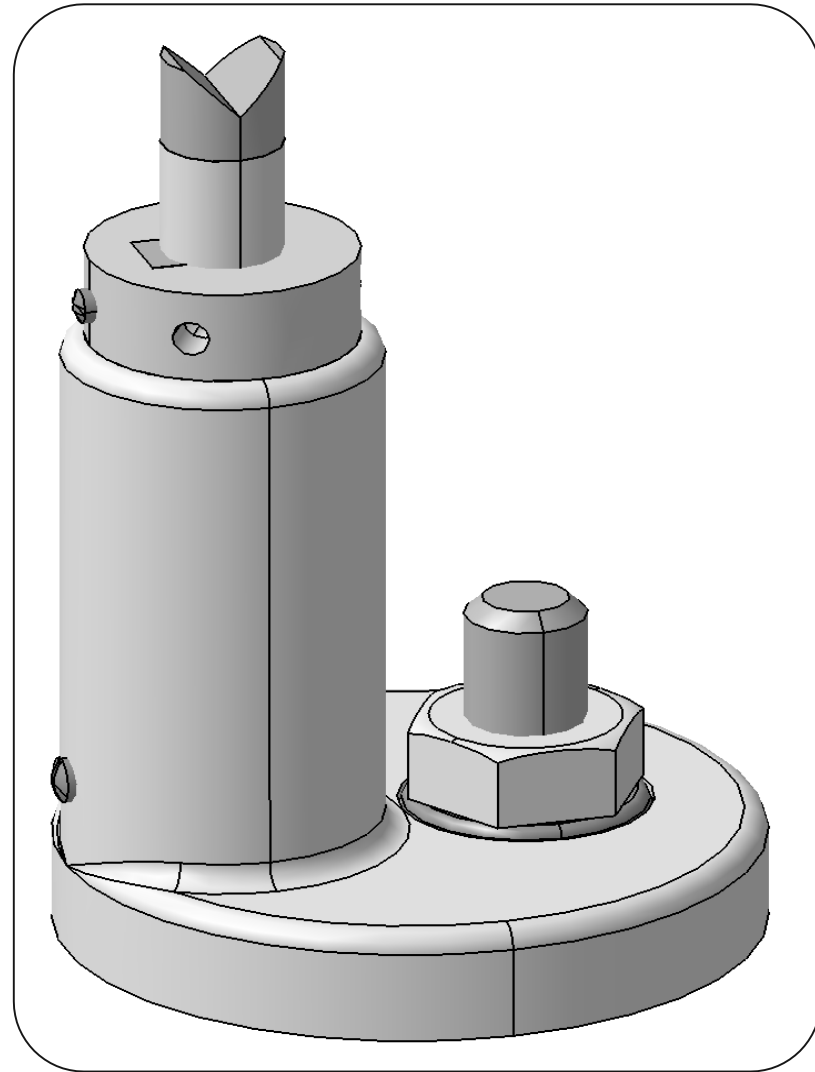
$$.50 + .0028 = .5028$$

➤ Shaft Limits =  $.50 - .0035 = .4965$

$$.50 - .0051 = .4949$$

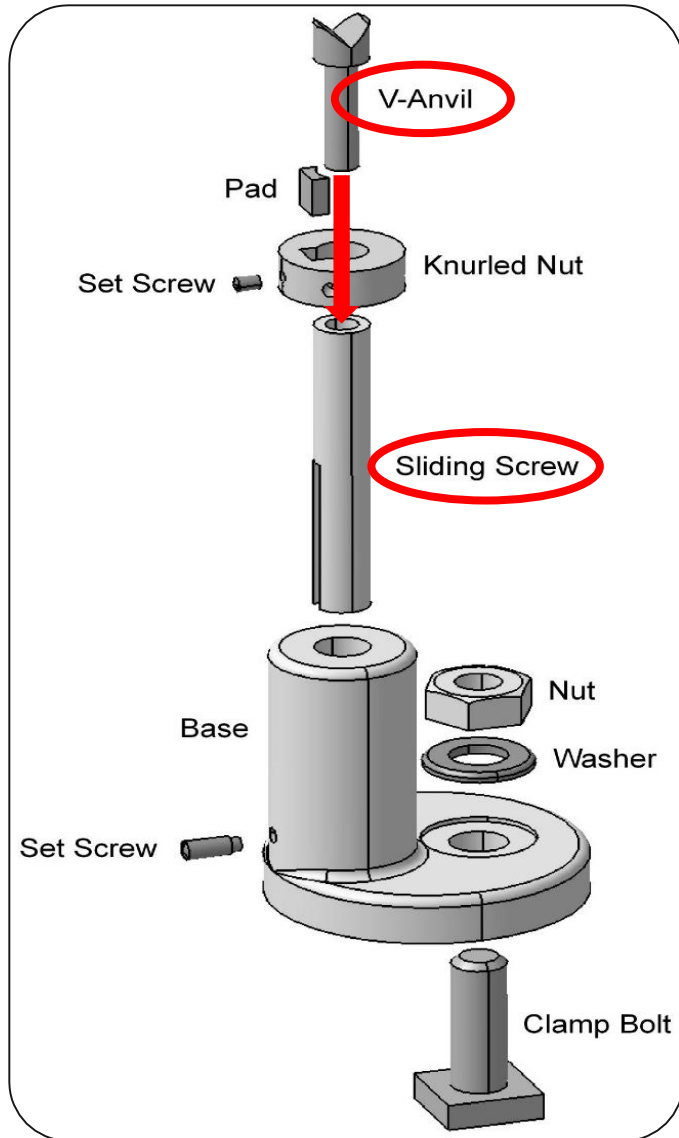
# Example 9

- Consider the **Milling Jack assembly** shown
  - Notice that there are **many parts that fit into or around other parts**
  - Each of these parts is **toleranced** to ensure **proper fit and function**



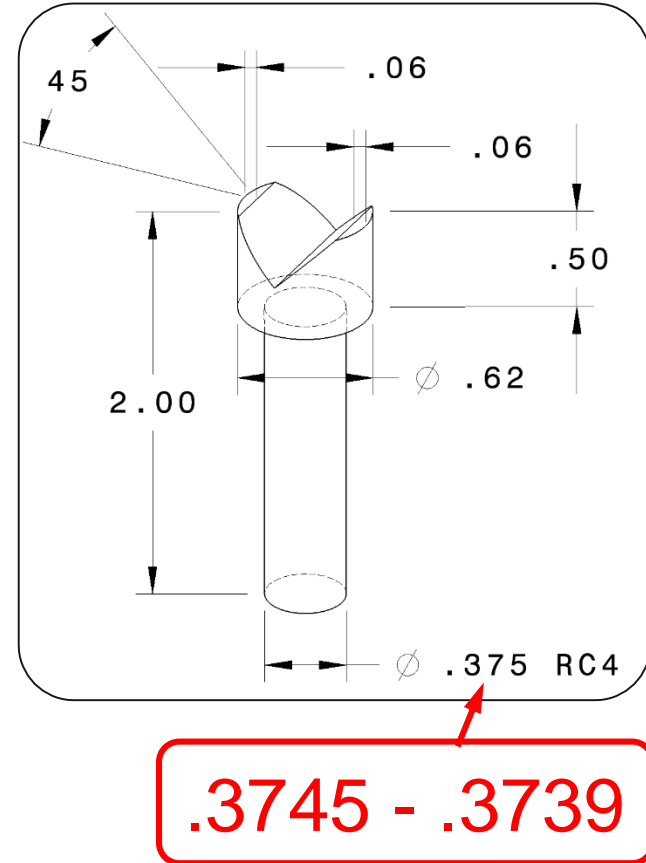
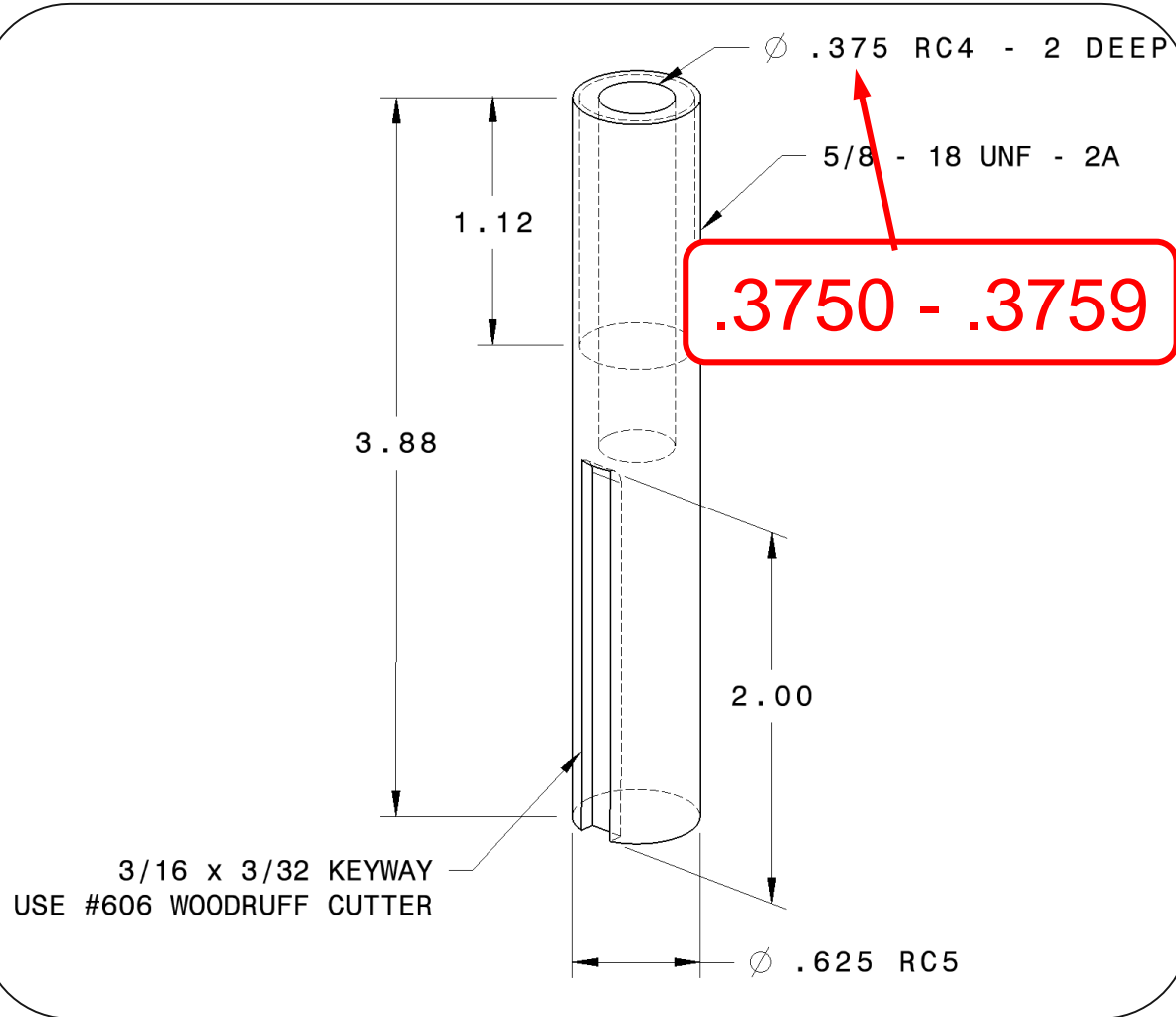
(K. Plantenberg , 2006, )

# Example 9

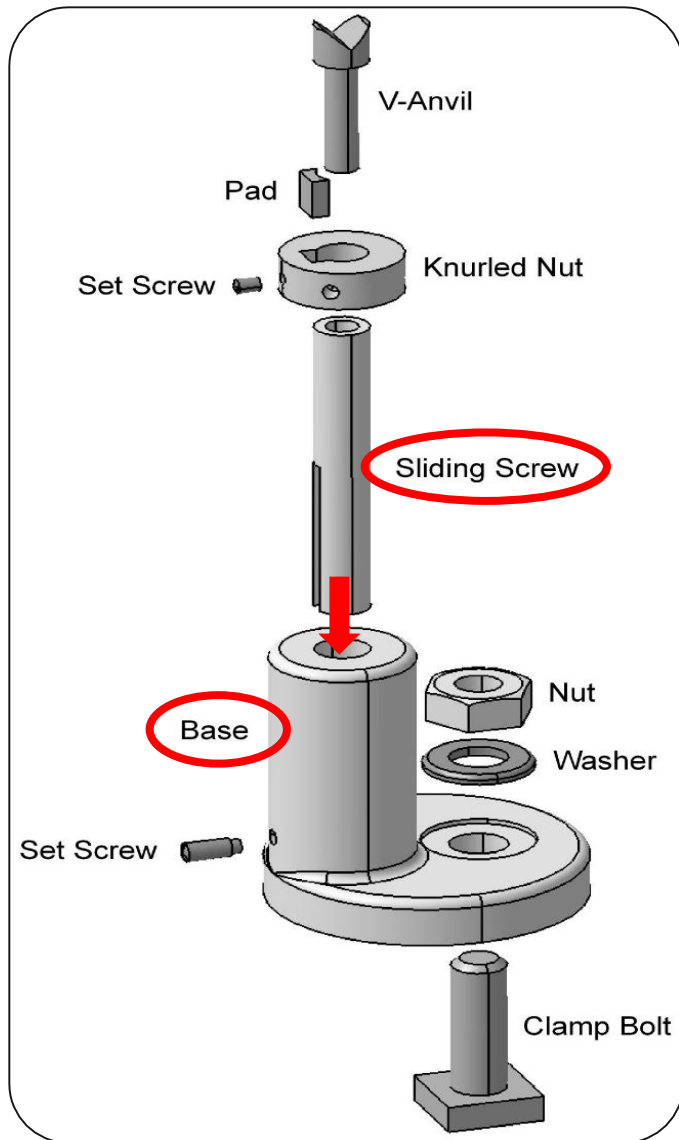


- The V-Anvil fits into the Sliding Screw with a RC4 fit
- The basic size is  $.375$  ( $3/8$ ). Determine the limits for both parts

# Example 9



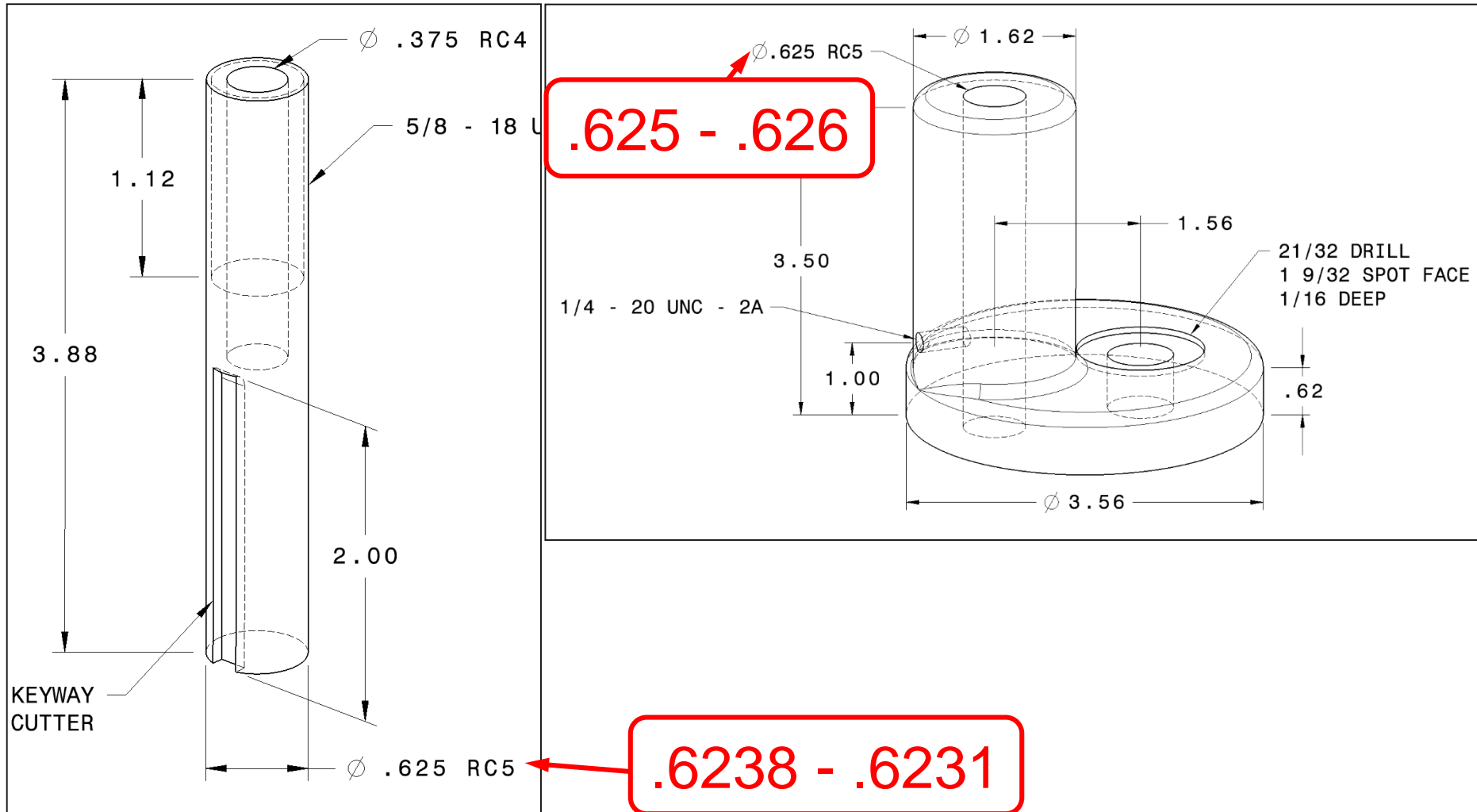
# Example 10



- The Sliding Screw fits into the Base with a RC5 fit
- The basic size is  $.625$  ( $5/8$ ). Determine the limits for both parts



# Example 10



# VI. Metric Tolerances

# Metric Tolerances Definitions

- Limits, Basic Size, Tolerance, MMC and LMC have the same definition as in the inch tolerance section

- **Upper deviation**

The upper deviation is the difference between the basic size and the permitted maximum size of the part

$$UD = |\text{basic size} - D_{\max}|$$

- **Lower deviation**

The lower deviation is the difference between the basic size and the minimum permitted size of the part

$$LD = |\text{basic size} - D_{\min}|$$

# Metric Tolerances Definitions

- **Fundamental deviation**

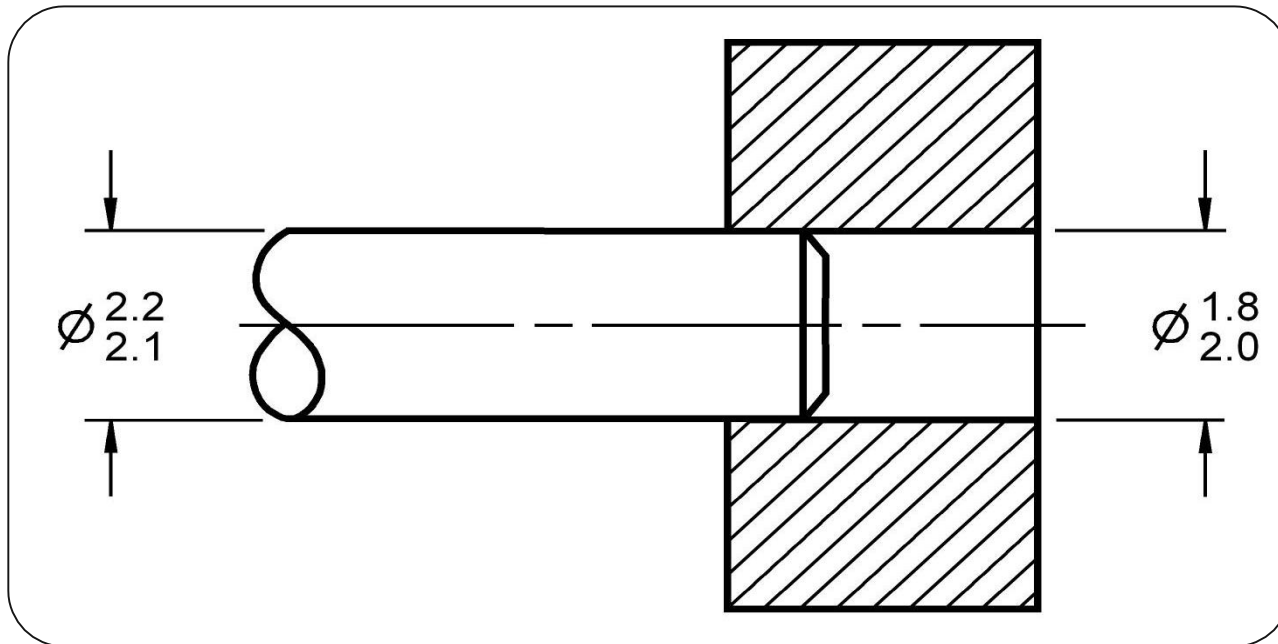
The fundamental deviation is the closest deviation to the basic size

- The fundamental deviation is the smaller of the UD and the LD
- A letter in the fit specification represents the fundamental deviation

Example: Metric Fit = H11/c11

# Exercise 1

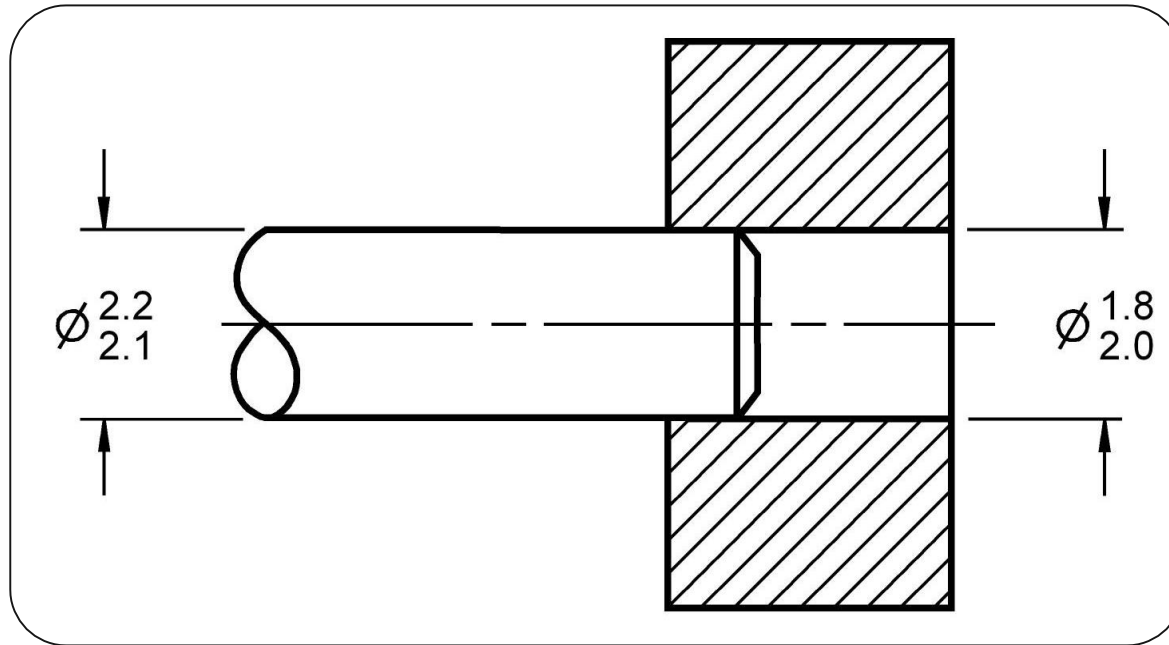
- Fill in the following table



|    | Shaft | Hole |
|----|-------|------|
| UD | 0.2   | 0    |
| LD | 0.1   | 0.2  |
| FD | 0.1   | 0    |

# Exercise 2

- Fill in the following table



| Type of fit | Interference |
|-------------|--------------|
|-------------|--------------|

# Metric Tolerances Definitions

- **International tolerance grade number (IT#)**

The IT#'s are a set of tolerances that vary according to the basic size and provide the same relative level of accuracy within a given grade

- The number in the fit specification represents the IT#
- A smaller number provides a smaller tolerance

# Metric Tolerances Definitions

- **Tolerance zone**

The fundamental deviation in combination with the IT# defines the tolerance zone

- The IT# establishes the magnitude of the tolerance zone or the amount that the dimension can vary
- The fundamental deviation establishes the position of the tolerance zone with respect to the basic size

*(K. Plantenberg , 2006, )*



# Available Metric Fits

| Hole Basis        | Shaft Basis       | Fit                     |
|-------------------|-------------------|-------------------------|
| H11/c11           | C11/h11           | Loose running           |
| H9/d9             | D9/h9             | Free running            |
| H8/f7             | F8/h7             | Close running           |
| H7/g6             | G7/h6             | Sliding                 |
| H7/h6             | H7/h6             | Locational clearance    |
| H7/k6 or<br>H7/n6 | K7/h6 or<br>N7/h6 | Locational transition   |
| H7/p6             | P7/h6             | Locational interference |
| H7/s6             | S7/h6             | Medium drive            |
| H7/u6             | U7/h6             | Force                   |

# Tolerance Designation

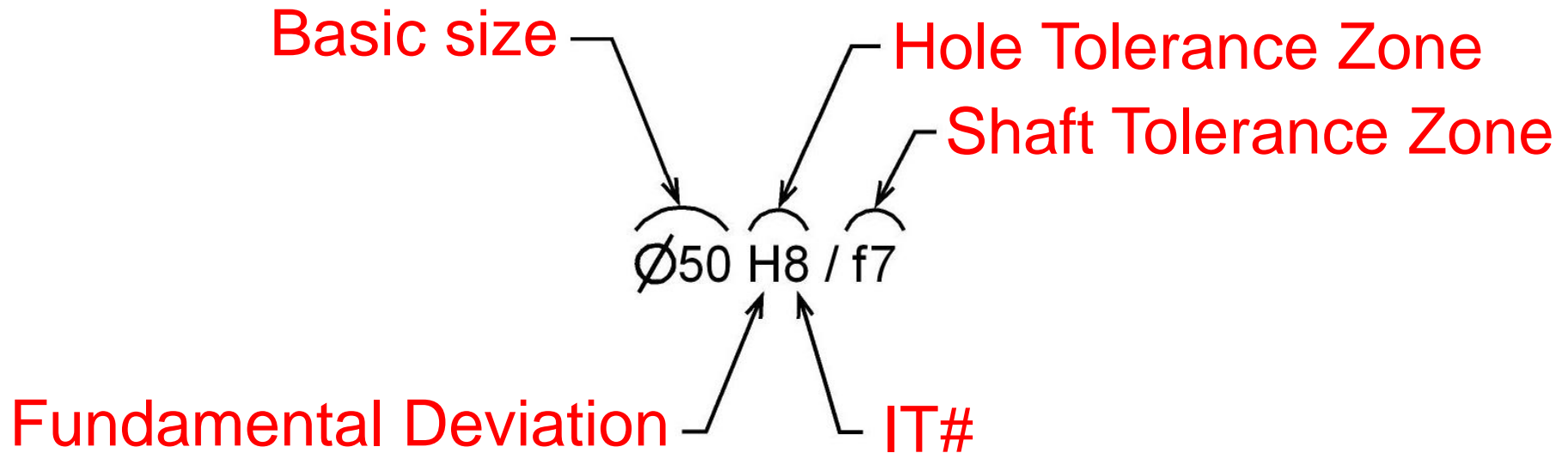
- A Metric fit is specified by stating the fundamental deviation and the IT#
- IT# = the amount that the dimension can vary (tolerance zone size)
- Fundamental deviation (letter) = establishes the position of the tolerance zone with respect to the basic size
- Hole = upper case
- Shaft = lower case

# Tolerance Designation

- Fits are specified by using the:
  - fundamental deviation (letter)
  - IT# (International Tolerance Grade #)
  
- When specifying the fit:
  - The hole = upper case letter
  - The shaft = lower case letter

# Example 11

- Fill in the appropriate name for the fit component



# Basic Hole / Basic Shaft Systems

- Metric limits and fits are divided into two different systems; the **basic hole system** and the **basic shaft system**
- **Basic hole system**: The basic hole system is used when you want the basic size to be attached to the hole dimension.
  - For example, if you want to tolerance a shaft based on a hole produced by a standard drill, reamer, broach, or another standard tool
- **Basic shaft system**: The basic shaft system is used when you want the basic size to be attached to the shaft dimension
  - For example, if you want to tolerance a hole based on the size of a purchased a standard drill rod

# Example 12

- Identify the type of fit and the system used to determine the limits of the following shaft and hole pairs

| Shaft           | Hole            | Type of Fit  | System |
|-----------------|-----------------|--------------|--------|
| 9.987 – 9.972   | 10.000 – 10.022 | Clearance    | Hole   |
| 60.021 – 60.002 | 60.000 – 60.030 | Transition   | Hole   |
| 40.000 – 39.984 | 39.924 – 39.949 | Interference | Shaft  |

(K. Plantenberg, 2006,)

# Example 13

- Find the limits, tolerance, type of fit, and type of system for a n30 H11/c11 fit

➤ Use the tolerance tables given below

| Basic Size | Loose Running |           | Free Running |          | Close Running |          | Sliding |          | Locational Clearance |          |
|------------|---------------|-----------|--------------|----------|---------------|----------|---------|----------|----------------------|----------|
|            | Hole H11      | Shaft c11 | Hole H9      | Shaft d9 | Hole H8       | Shaft f7 | Hole H7 | Shaft g6 | Hole H7              | Shaft h6 |
| 1 max      | 1.060         | 0.940     | 1.025        | 0.980    | 1.014         | 0.994    | 1.010   | 0.998    | 1.010                | 1.000    |
| 1 min      | 1.000         | 0.880     | 1.000        | 0.955    | 1.000         | 0.984    | 1.000   | 0.992    | 1.000                | 0.994    |
| 1.2 max    | 1.260         | 1.140     | 1.225        | 1.180    | 1.214         | 1.194    | 1.210   | 1.198    | 1.210                | 1.200    |
| 1.2 min    | 1.200         | 1.080     | 1.200        | 1.155    | 1.200         | 1.184    | 1.200   | 1.192    | 1.200                | 1.194    |
| 1.6 max    | 1.660         | 1.540     | 1.625        | 1.580    | 1.614         | 1.594    | 1.610   | 1.598    | 1.610                | 1.600    |
| 1.6 min    | 1.600         | 1.480     | 1.600        | 1.555    | 1.600         | 1.584    | 1.600   | 1.592    | 1.600                | 1.594    |
| 2 max      | 2.060         | 1.940     | 2.025        | 1.980    | 2.014         | 1.994    | 2.010   | 1.998    | 2.010                | 2.000    |
| 2 min      | 2.000         | 1.880     | 2.000        | 1.955    | 2.000         | 1.984    | 2.000   | 1.992    | 2.000                | 1.994    |

|        |        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 16 max | 16.110 | 15.905 | 16.043 | 15.950 | 16.027 | 15.984 | 16.018 | 15.994 | 16.018 | 16.000 |
| 16 min | 16.000 | 15.795 | 16.000 | 15.907 | 16.000 | 15.966 | 16.000 | 15.983 | 16.000 | 15.989 |
| 20 max | 20.130 | 19.890 | 20.052 | 19.935 | 20.033 | 19.980 | 20.021 | 19.993 | 20.021 | 20.000 |
| 20 min | 20.000 | 19.760 | 20.000 | 19.883 | 20.000 | 19.959 | 20.000 | 19.980 | 20.000 | 19.987 |
| 25 max | 25.130 | 24.890 | 25.052 | 24.935 | 25.033 | 24.980 | 25.021 | 24.993 | 25.021 | 25.000 |
| 25 min | 25.000 | 24.760 | 25.000 | 24.883 | 25.000 | 24.959 | 25.000 | 24.980 | 25.000 | 24.987 |
| 30 max | 30.130 | 29.890 | 30.052 | 29.935 | 30.033 | 29.980 | 30.021 | 29.993 | 30.021 | 30.000 |
| 30 min | 30.000 | 29.760 | 30.000 | 29.883 | 30.000 | 29.959 | 30.000 | 29.980 | 30.000 | 29.987 |

# Example 14

- Find the limits, tolerance, type of fit, and type of system for a n30 H11/c11 fit.

|           | Shaft                     | Hole            |
|-----------|---------------------------|-----------------|
| Limits    | 29.890 – 29.760           | 30.000 – 30.130 |
| Tolerance | 0.13                      | 0.13            |
| System    | Hole                      |                 |
| Fit       | Clearance – Loose Running |                 |



# Example 15

- Find the limits, tolerance, type of fit, and type of system for a n30 P7/h6 fit
  - Use the tolerance tables given below

| Basic Size | Locational Transition |          | Locational Transition |          | Locational Interference |          | Medium Drive |          | Force   |          |
|------------|-----------------------|----------|-----------------------|----------|-------------------------|----------|--------------|----------|---------|----------|
|            | Hole K7               | Shaft h6 | Hole N7               | Shaft h6 | Hole P7                 | Shaft h6 | Hole S7      | Shaft h6 | Hole U7 | Shaft h6 |
| 1 max      | 1.000                 | 1.000    | 0.996                 | 1.000    | 0.994                   | 1.000    | 0.986        | 1.000    | 0.982   | 1.000    |
| 1 min      | 0.990                 | 0.994    | 0.986                 | 0.994    | 0.984                   | 0.994    | 0.976        | 0.994    | 0.972   | 0.994    |
| 1.2 max    | 1.200                 | 1.200    | 1.196                 | 1.200    | 1.194                   | 1.200    | 1.186        | 1.200    | 1.182   | 1.200    |
| 1.2 min    | 1.190                 | 1.194    | 1.186                 | 1.194    | 1.184                   | 1.194    | 1.176        | 1.194    | 1.172   | 1.194    |
| 1.6 max    | 1.600                 | 1.600    | 1.596                 | 1.600    | 1.594                   | 1.600    | 1.586        | 1.600    | 1.582   | 1.600    |
| 1.6 min    | 1.590                 | 1.594    | 1.586                 | 1.594    | 1.584                   | 1.594    | 1.576        | 1.594    | 1.572   | 1.594    |
| 2 max      | 2.000                 | 2.000    | 1.996                 | 2.000    | 1.994                   | 2.000    | 1.986        | 2.000    | 1.982   | 2.000    |
| 2 min      | 1.990                 | 1.994    | 1.986                 | 1.994    | 1.984                   | 1.994    | 1.976        | 1.994    | 1.972   | 1.994    |
| 16 max     | 16.006                | 16.000   | 15.995                | 16.000   | 15.989                  | 16.000   | 15.979       | 16.000   | 15.974  | 16.000   |
| 16 min     | 15.988                | 15.989   | 15.977                | 15.989   | 15.971                  | 15.989   | 15.961       | 15.989   | 15.956  | 15.989   |
| 20 max     | 20.006                | 20.000   | 19.993                | 20.000   | 19.986                  | 20.000   | 19.973       | 20.000   | 19.967  | 20.000   |
| 20 min     | 19.985                | 19.987   | 19.972                | 19.987   | 19.965                  | 19.987   | 19.952       | 19.987   | 19.946  | 19.987   |
| 25 max     | 25.006                | 25.000   | 24.993                | 25.000   | 24.986                  | 25.000   | 24.973       | 25.000   | 24.960  | 25.000   |
| 25 min     | 24.985                | 24.987   | 24.972                | 24.987   | 24.965                  | 24.987   | 24.952       | 24.987   | 24.939  | 24.987   |
| 30 max     | 30.006                | 30.000   | 29.993                | 30.000   | 29.986                  | 30.000   | 29.973       | 30.000   | 29.960  | 30.000   |
| 30 min     | 29.985                | 29.987   | 29.972                | 29.987   | 29.965                  | 29.987   | 29.952       | 29.987   | 29.939  | 29.987   |

# Example 16

- Find the limits, tolerance, type of fit, and type of system for a n30 P7/h6 fit

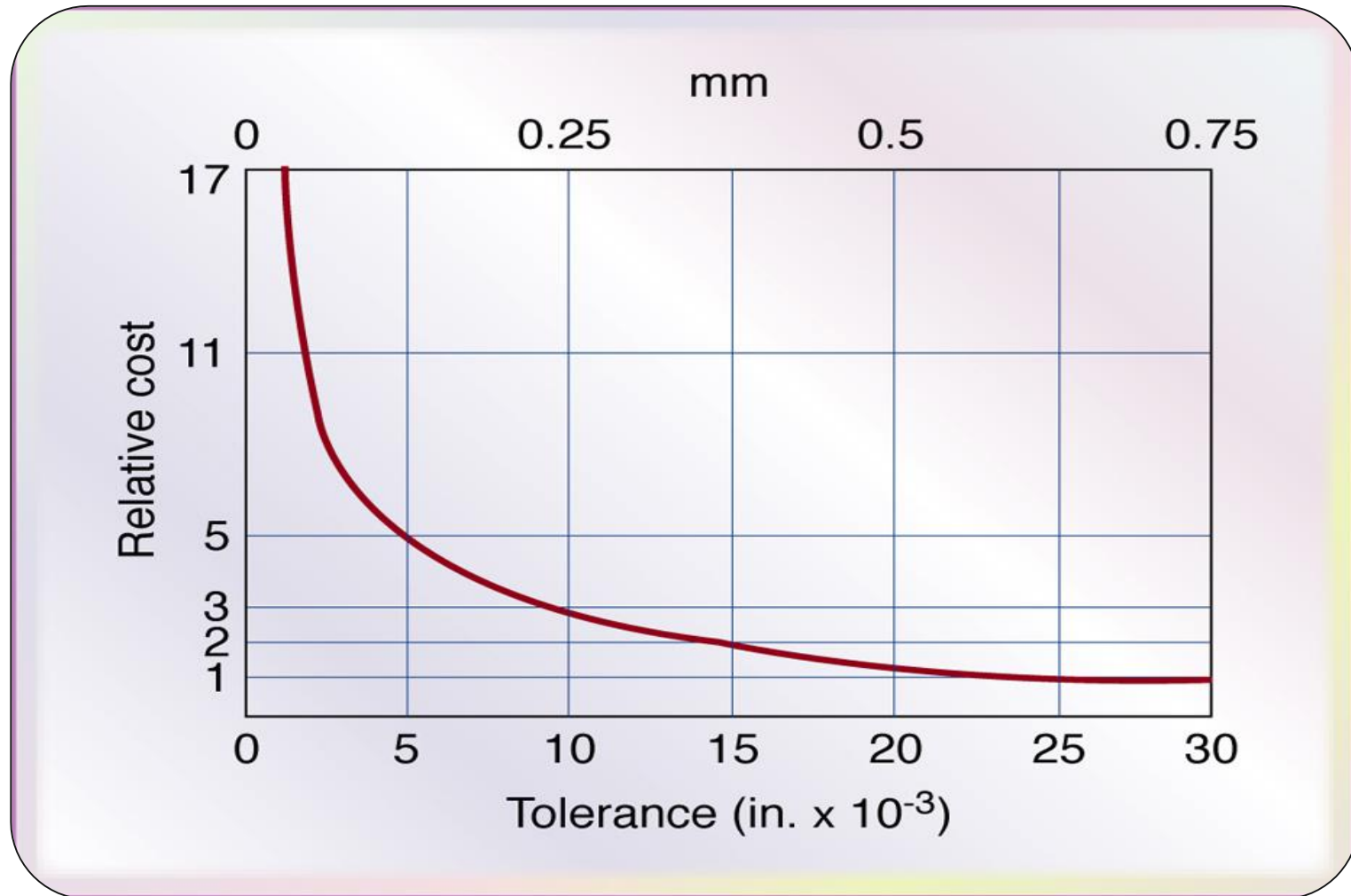
|           | Shaft                   | Hole            |
|-----------|-------------------------|-----------------|
| Limits    | 30.000 – 29.987         | 29.965 – 29.986 |
| Tolerance | 0.013                   | 0.021           |
| System    | Shaft                   |                 |
| Fit       | Locational Interference |                 |

# VII. Selecting Tolerances

# Selecting Tolerances

- **Tolerances** will govern the method of manufacturing
  - When the **tolerances are reduced**, the **cost** of manufacturing **rises very rapidly**
  - Specify **as generous a tolerance as possible** without interfering with the function of the part

# Selecting Tolerances



**Figure 4: Dependence of manufacturing cost on dimensional tolerances**

(source: Manufacturing, Engineering & Technology, Fifth Edition, by S. Kalpakjian and Steven R. Schmid )

# Selecting Tolerances

- Choosing the most appropriate tolerance depends on many factors such as:
  - **Length of engagement**
  - **Bearing load**
  - **Speed**
  - **Lubrication**
  - **Temperature**
  - **Humidity**
  - **Material**
- **Experience** also plays a significant role

# Machining and IT Grades

| Machining Operation  | IT Grades |   |   |   |   |   |    |    |
|----------------------|-----------|---|---|---|---|---|----|----|
|                      | 4         | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| Lapping & Honing     | ■         | ■ |   |   |   |   |    |    |
| Cylindrical Grinding |           | ■ | ■ | ■ |   |   |    |    |
| Surface Grinding     |           | ■ | ■ | ■ | ■ |   |    |    |
| Diamond Turning      |           | ■ | ■ | ■ |   |   |    |    |
| Diamond Boring       |           | ■ | ■ | ■ |   |   |    |    |
| Broaching            |           | ■ | ■ | ■ | ■ |   |    |    |
| Reaming              |           |   | ■ | ■ | ■ | ■ | ■  |    |
| Turning              |           |   |   | ■ | ■ | ■ | ■  | ■  |
| Boring               |           |   |   |   | ■ | ■ | ■  | ■  |
| Milling              |           |   |   |   |   |   | ■  | ■  |
| Planing & Shaping    |           |   |   |   |   |   | ■  | ■  |
| Drilling             |           |   |   |   |   |   | ■  | ■  |
| Punching             |           |   |   |   |   |   | ■  | ■  |
| Die Casting          |           |   |   |   |   |   |    | ■  |

# VIII.Tolerance Accumulation



# Tolerance Accumulation

- Figures 5-7 compare the tolerance values resulting from the following **three methods of dimensioning**

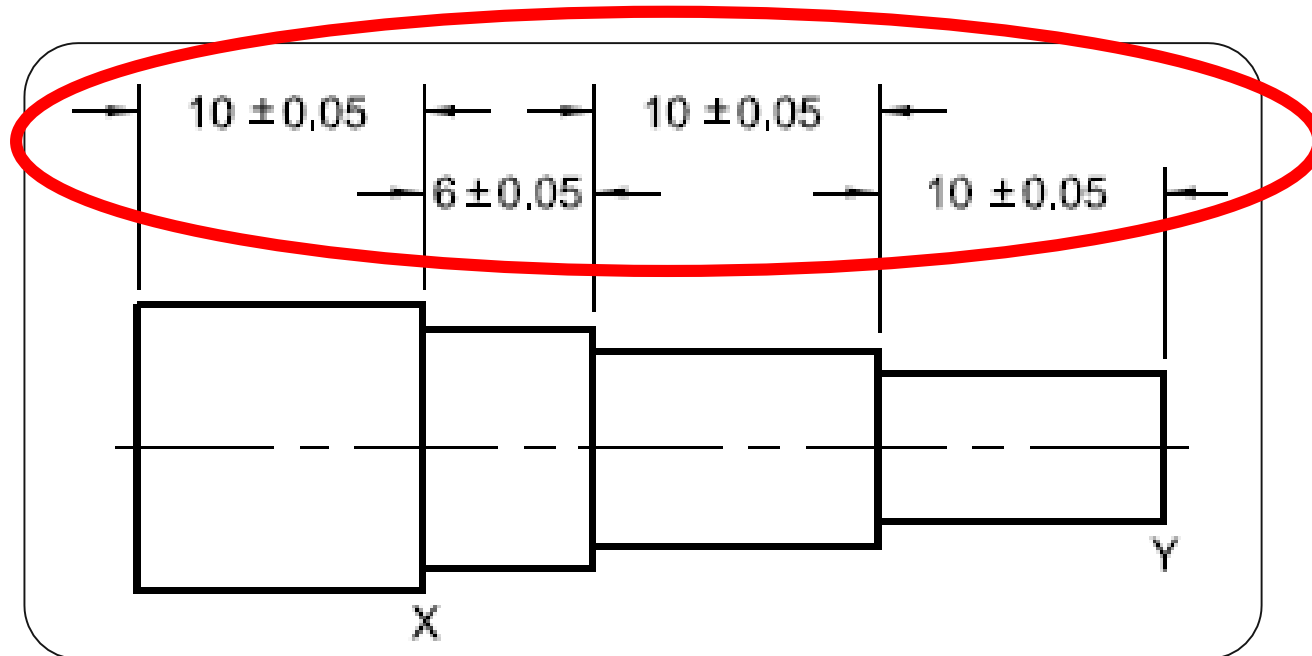


Figure 5: Chain Dimensioning-Greatest tolerance accumulation between X and Y

**(a) Chain Dimensioning:** The maximum variation between two features is equal to the sum of the tolerances on the intermediate distances; this results in the greatest tolerance accumulation. In this figure the tolerance accumulation between surfaces X and Y is  $\pm 0.15$

(K. Plantenberg, 2006,)

# Tolerance Accumulation

**(b) Base Line Dimensioning:** The maximum variation between two features is equal to the sum of the tolerances on the two dimensions from their origin to the features; this results in a reduction of the tolerance accumulation. In this figure, the tolerance accumulation between surfaces X and Y is  $\pm 0.1$

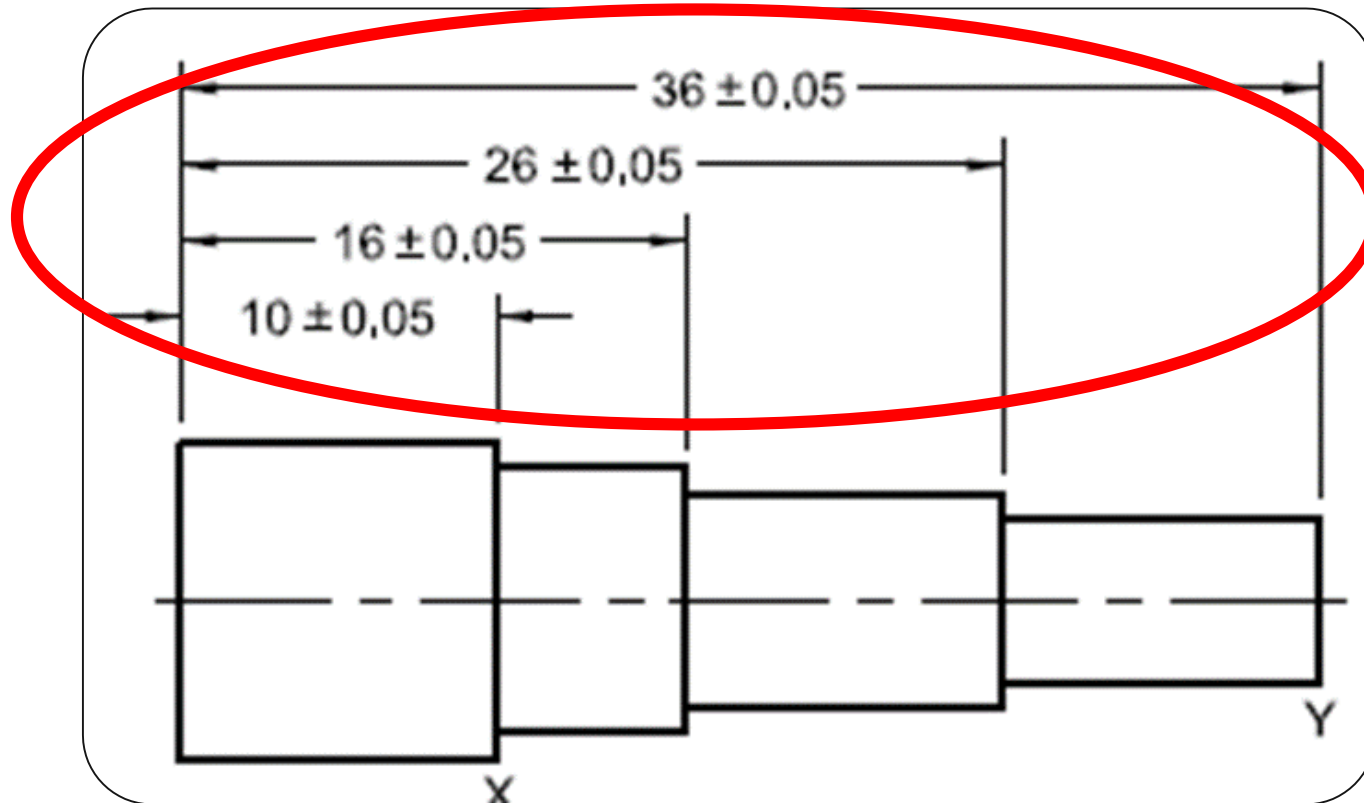


Figure 6: Base Line Dimensioning-Lesser tolerance accumulation between X and Y

# Tolerance Accumulation

**(c) Direct Dimensioning:** The maximum variation between two features is controlled by the tolerance on the dimension between the features; this results in the least tolerance. In this figure, the tolerance between surfaces X and Y is  $\pm 0.05$

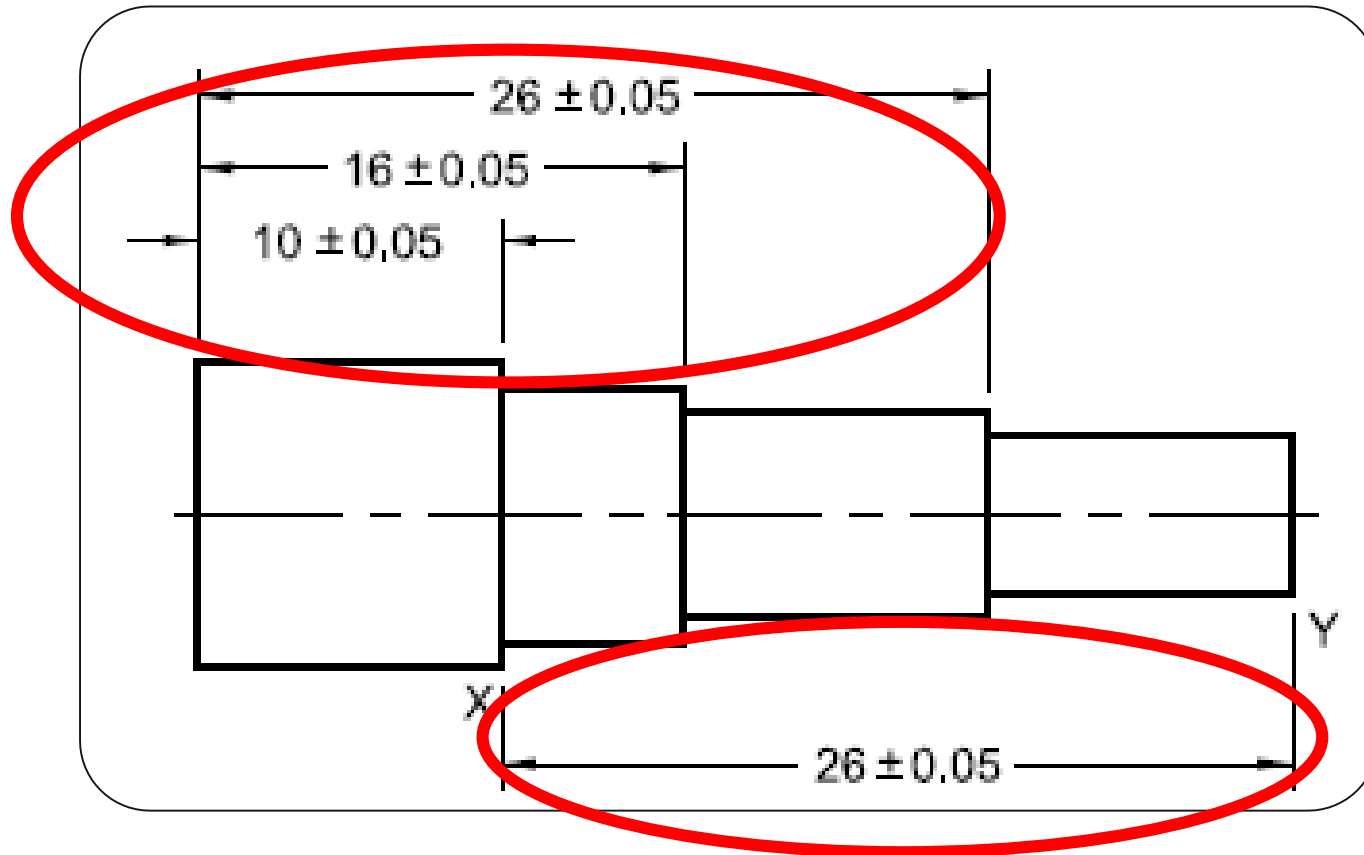
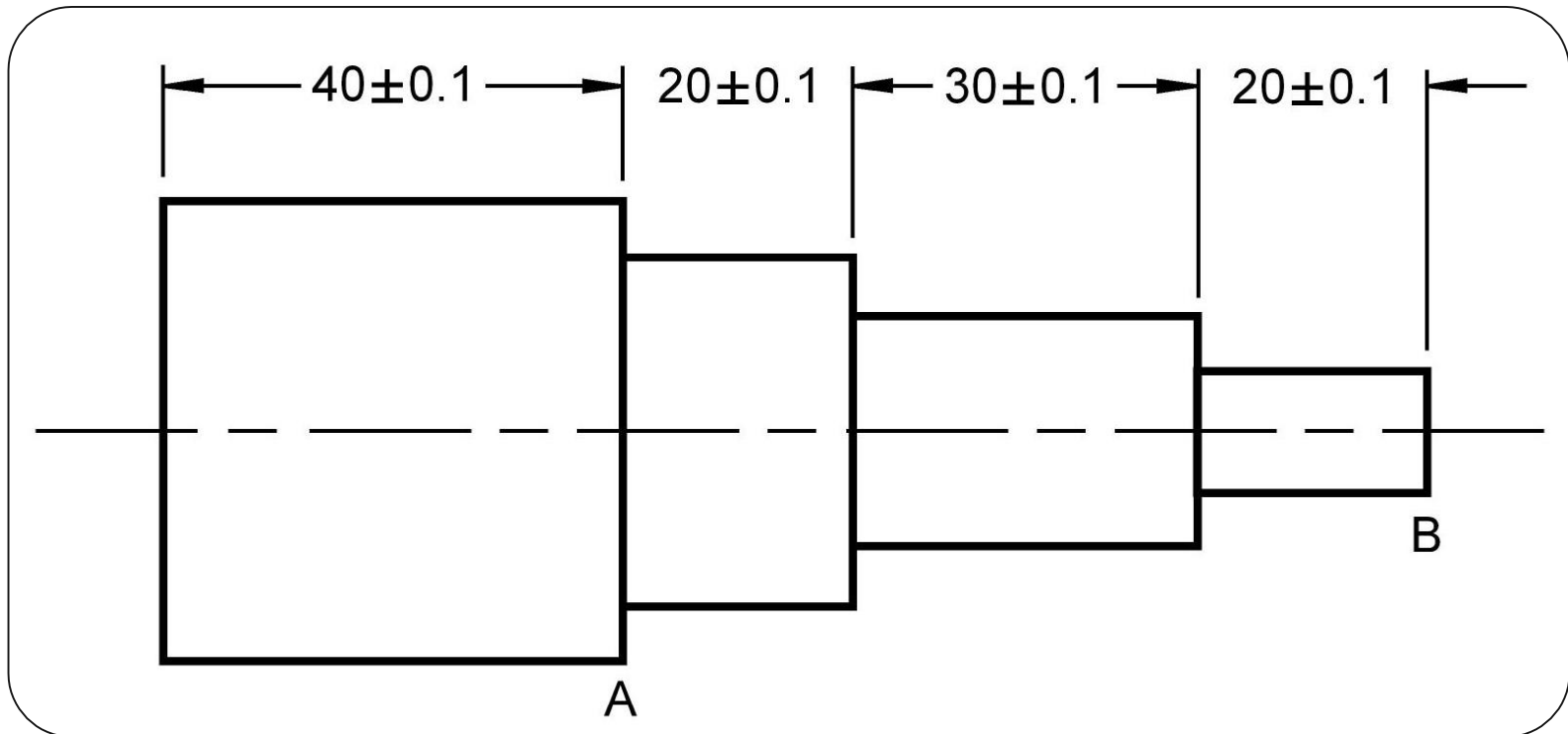


Figure 7 :Direct Dimensioning-Least tolerance between X and Y

(K. Plantenberg , 2006, )

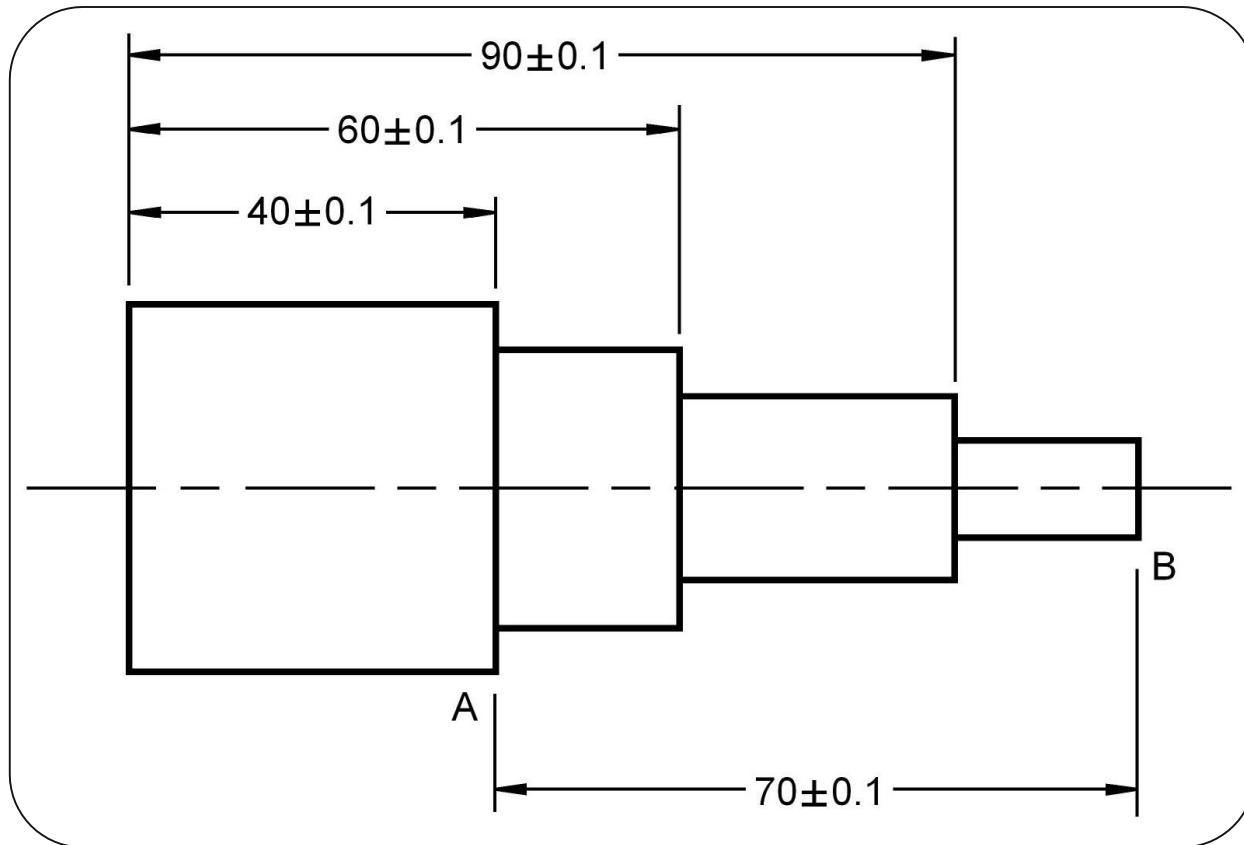
# Tolerance Accumulation

- The **tolerance** between two features of a part depends on the number of controlling dimensions



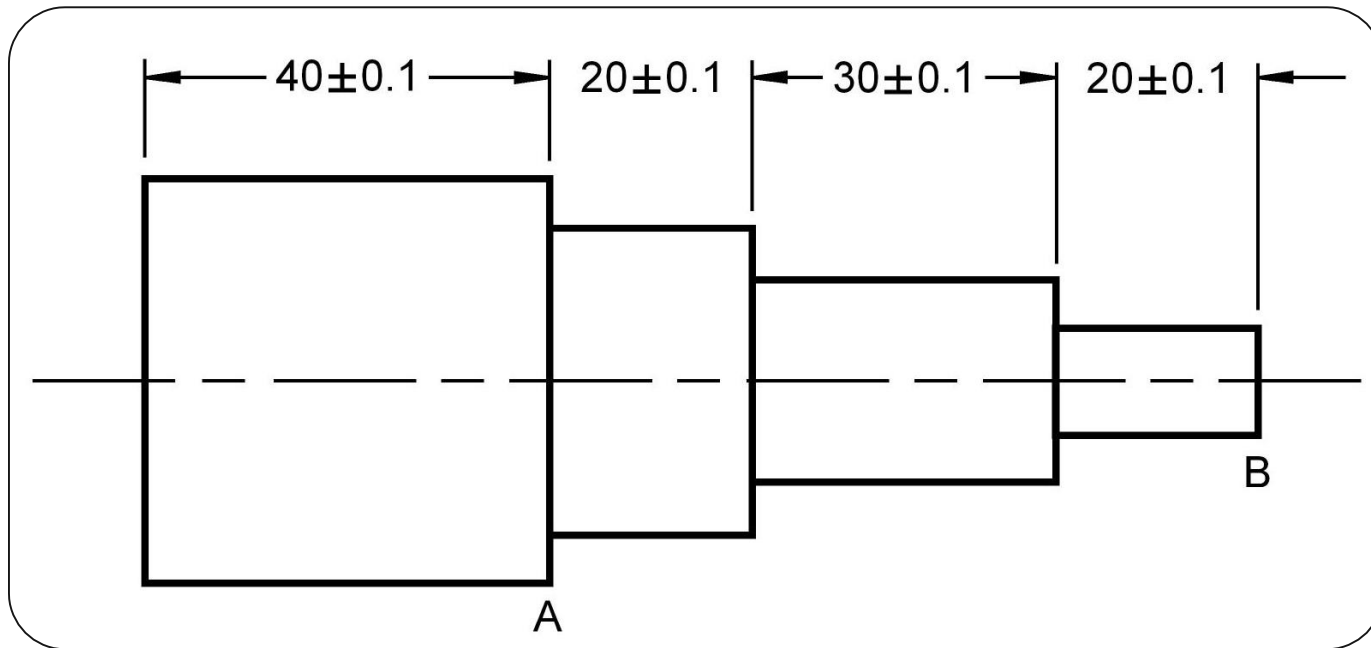
# Tolerance Accumulation

- The **distance** could be controlled by a **single dimension** or **multiple dimensions**



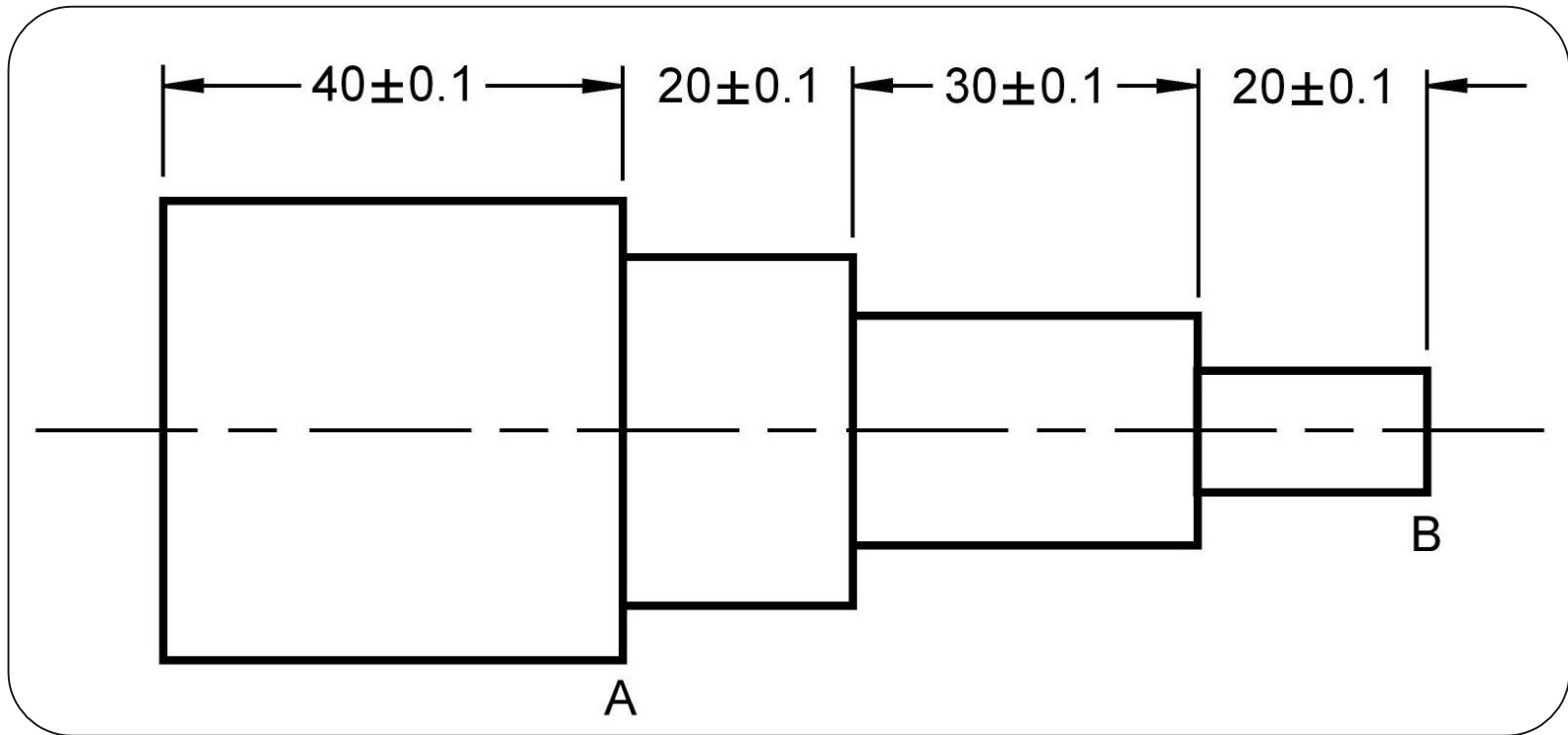
# Tolerance Accumulation

- The **maximum variation** between two features is equal to the **sum of the tolerances placed on the controlling dimensions**



# Tolerance Accumulation

- As the number of controlling dimensions **increases**, the tolerance accumulation **increases**



# Tolerance Accumulation

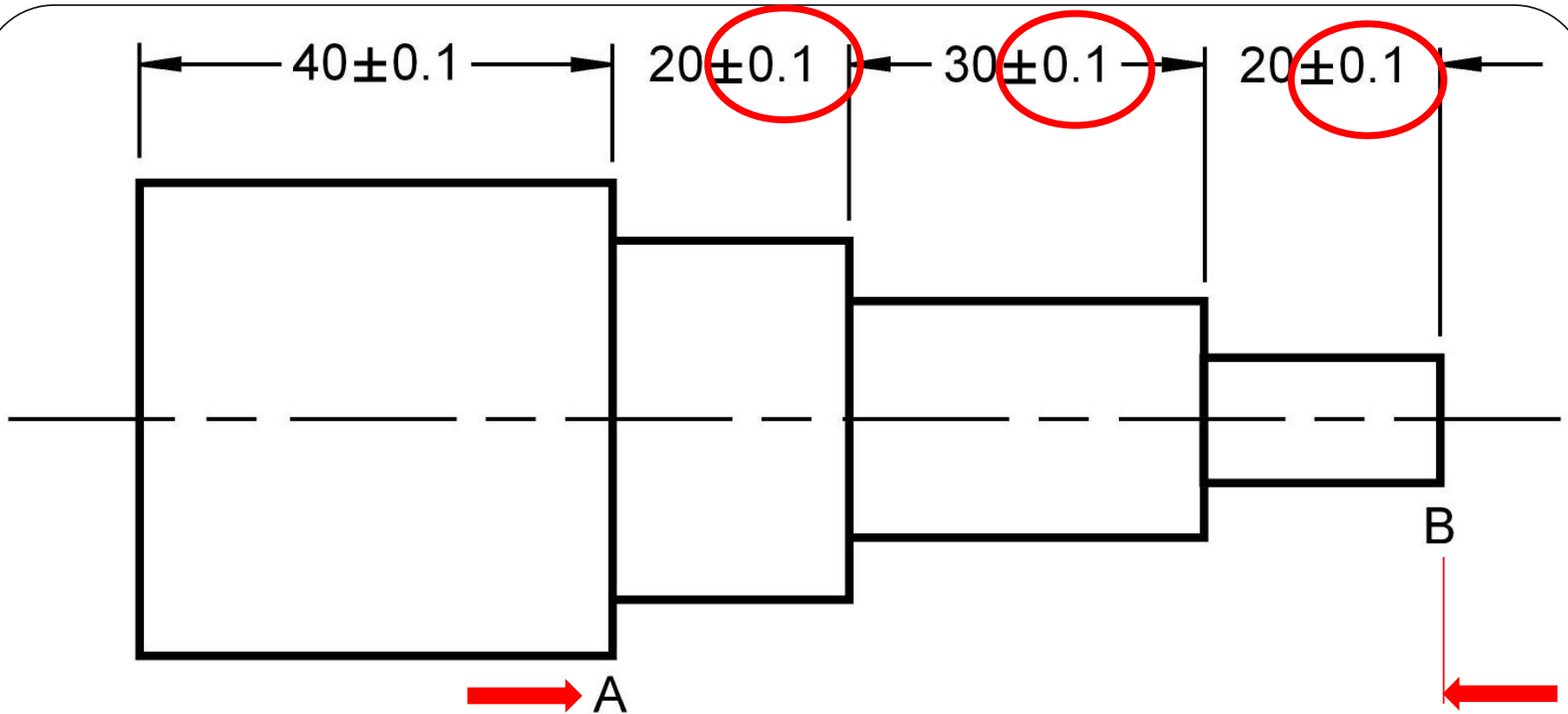
- **Remember:** even if the dimension does not have a stated tolerance, it has an implied tolerance

- **Example:**

What is the tolerance accumulation for the distance between surface A and B for the following three dimensioning methods?



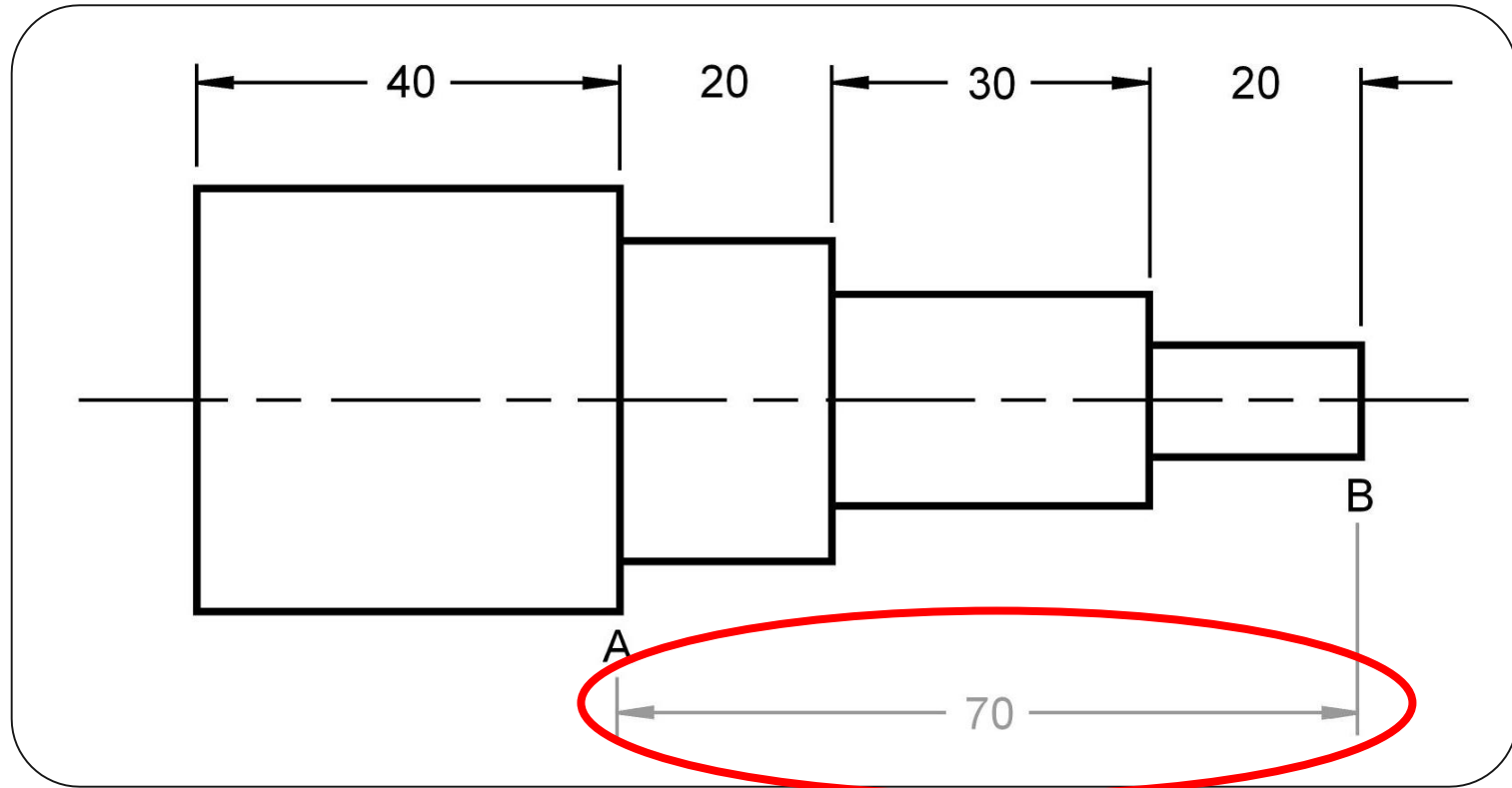
# Tolerance Accumulation



Tolerance accumulation between surface A and B = **0.3**

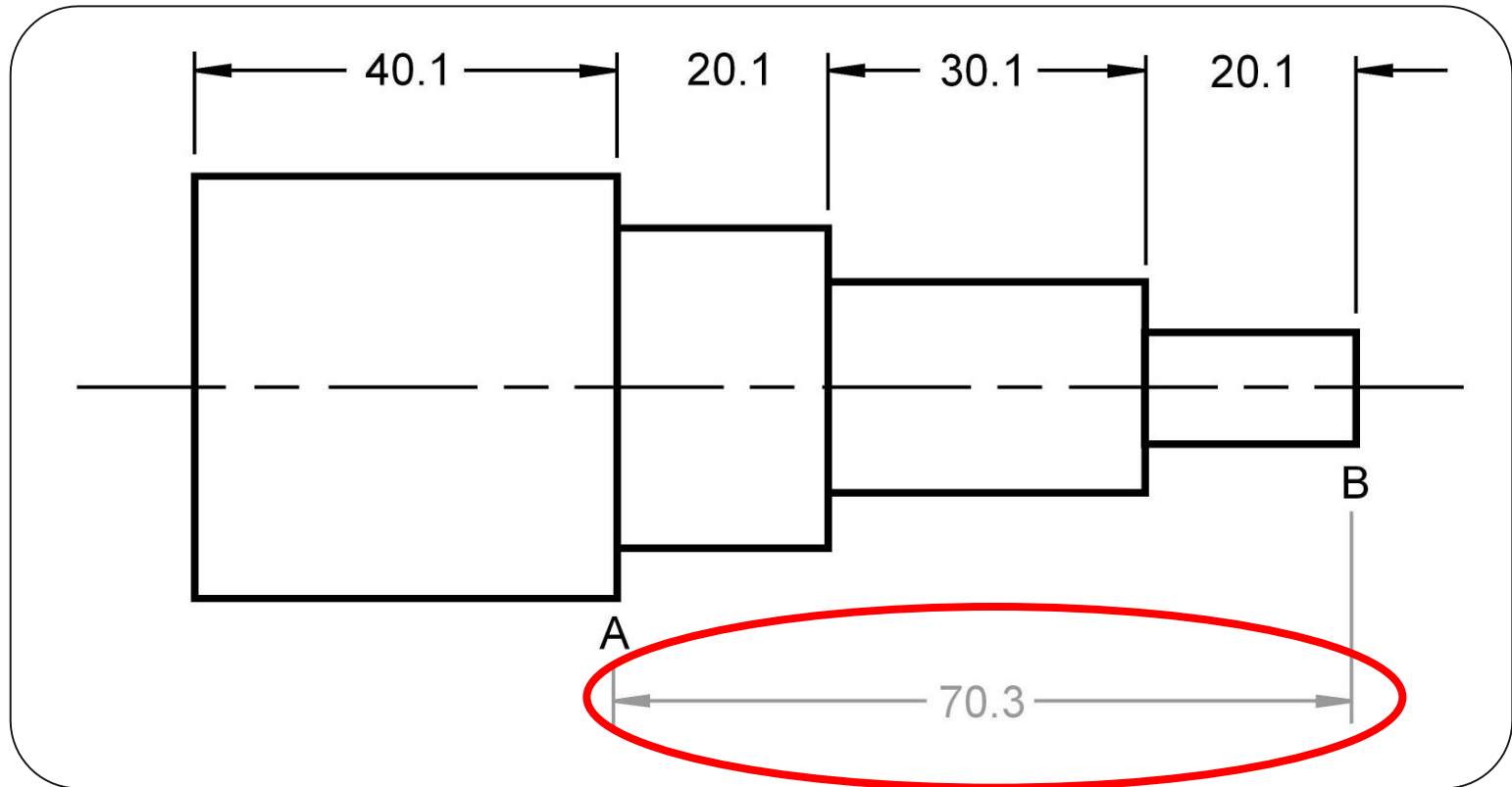
(K. Plantenberg, 2006,)

# Tolerance Accumulation



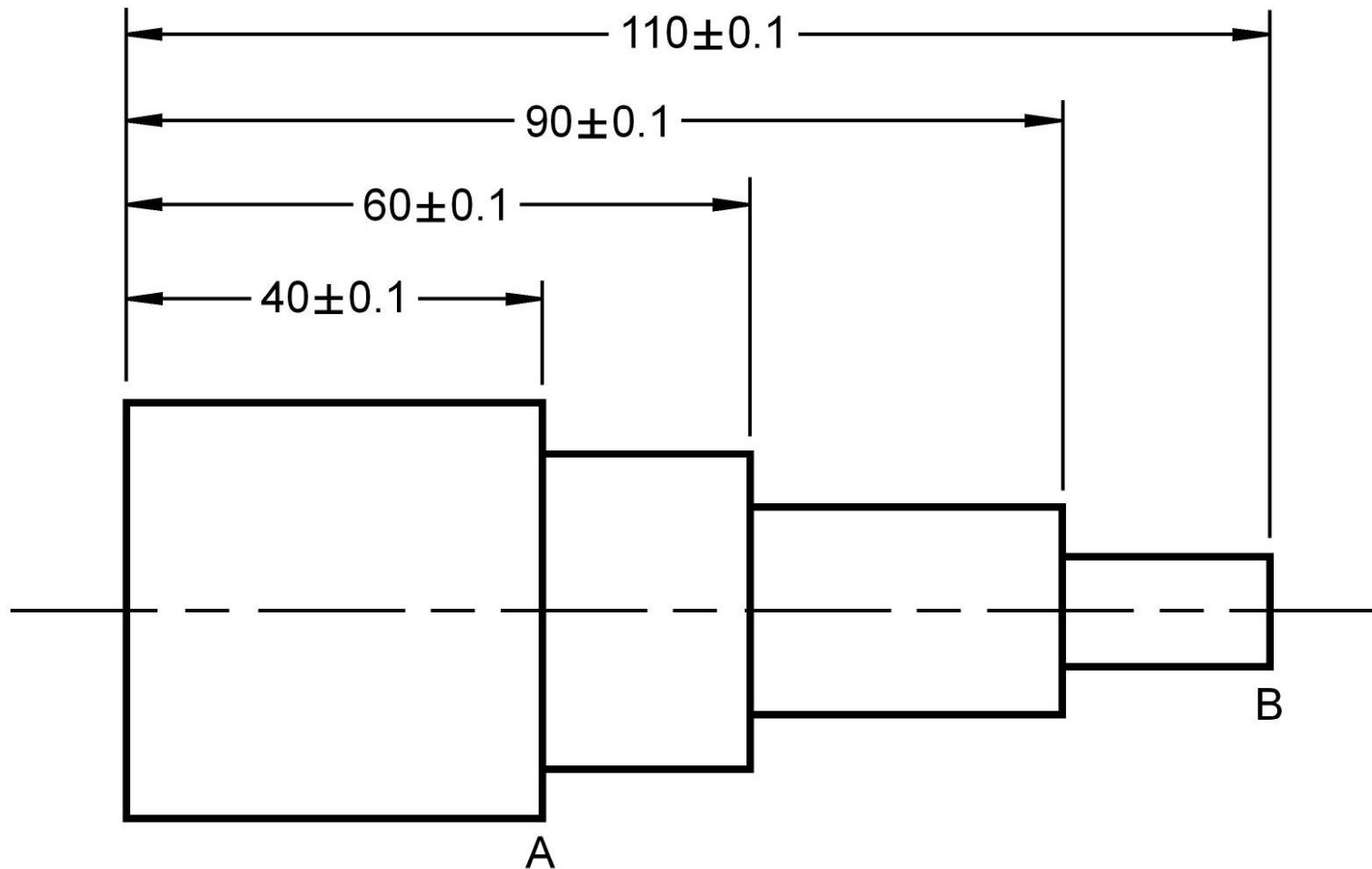
**Perfect**

# Tolerance Accumulation



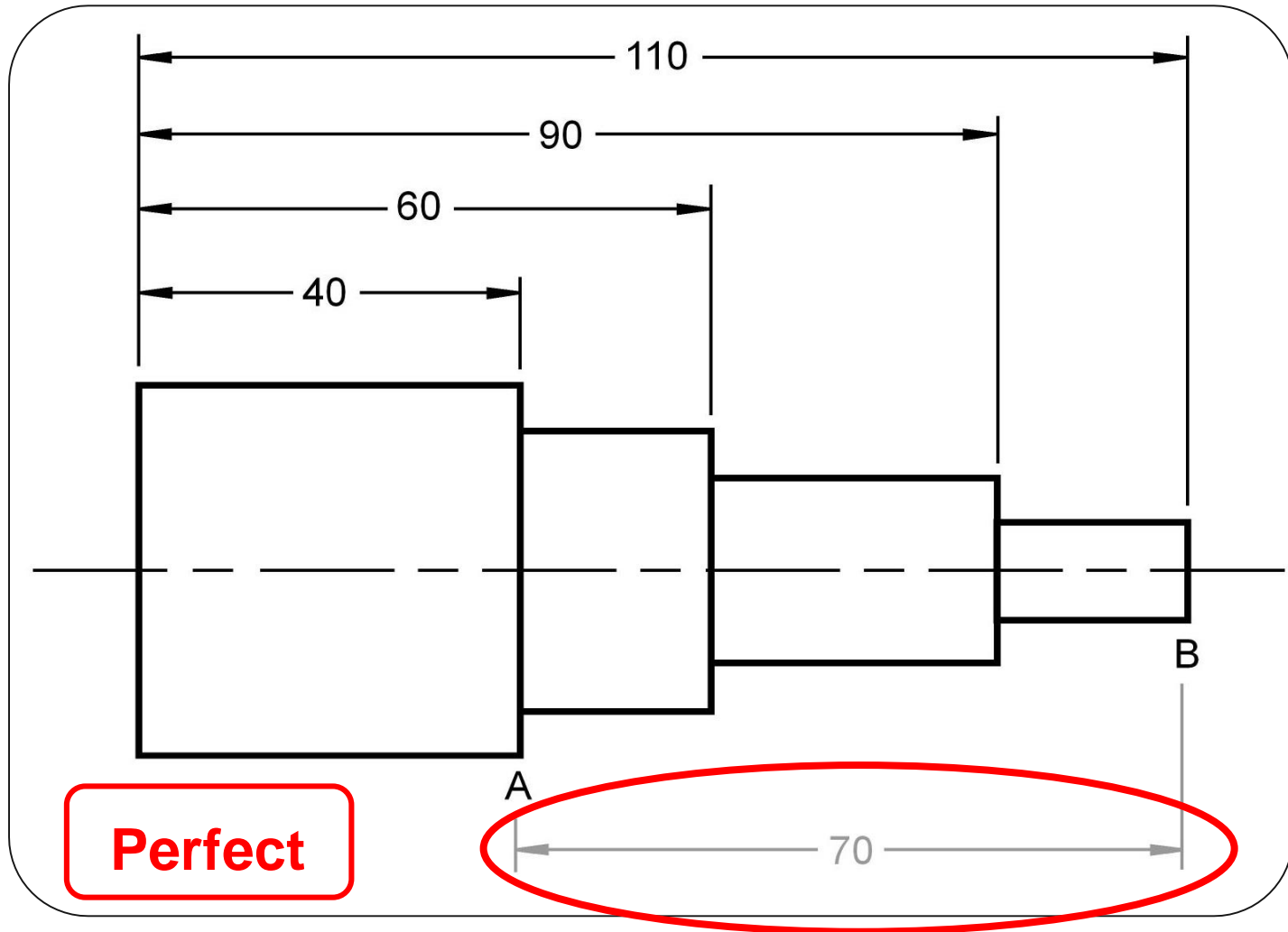
**Worst Case**

# Tolerance Accumulation

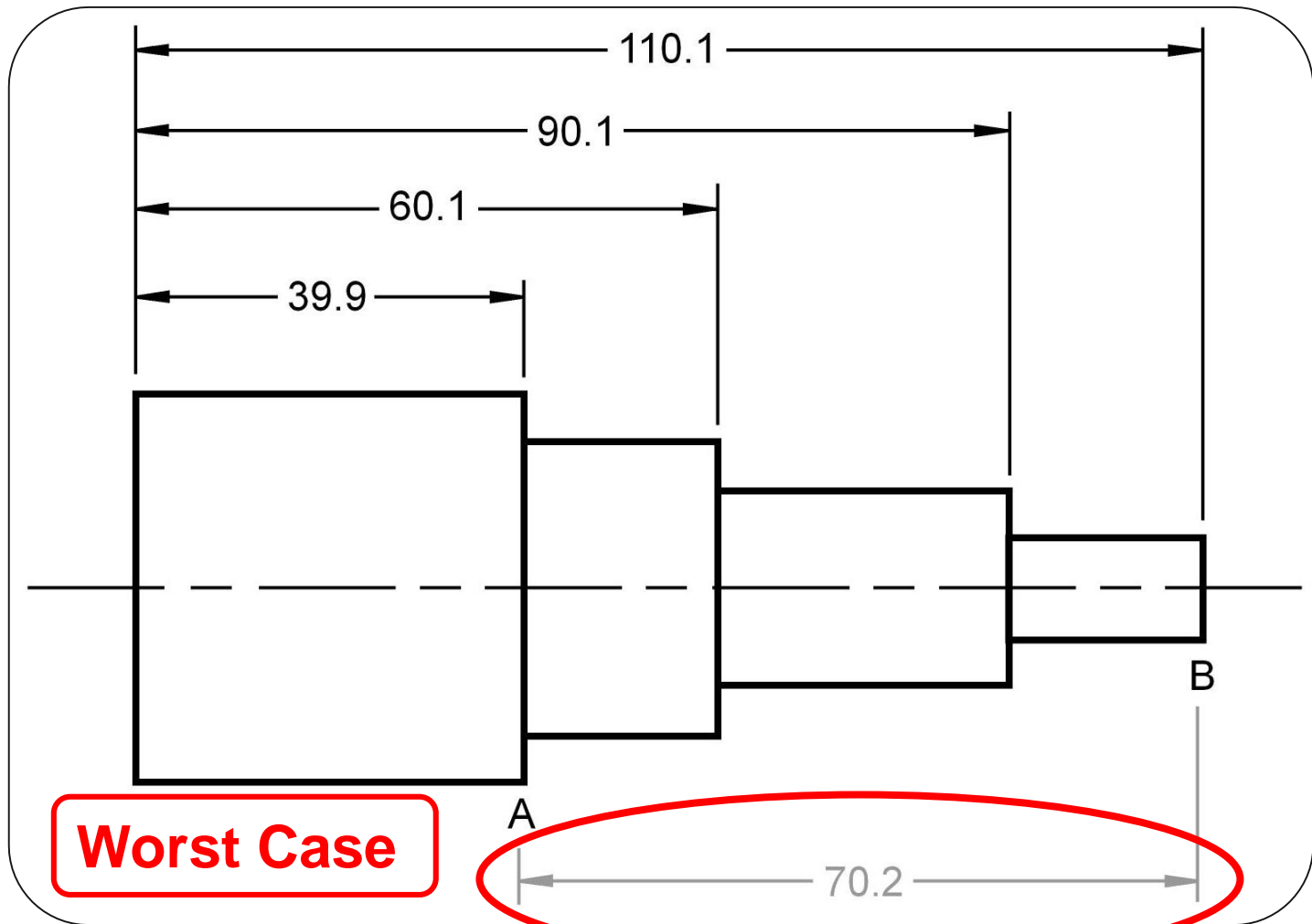


Tolerance accumulation between surface A and B = **0.2**

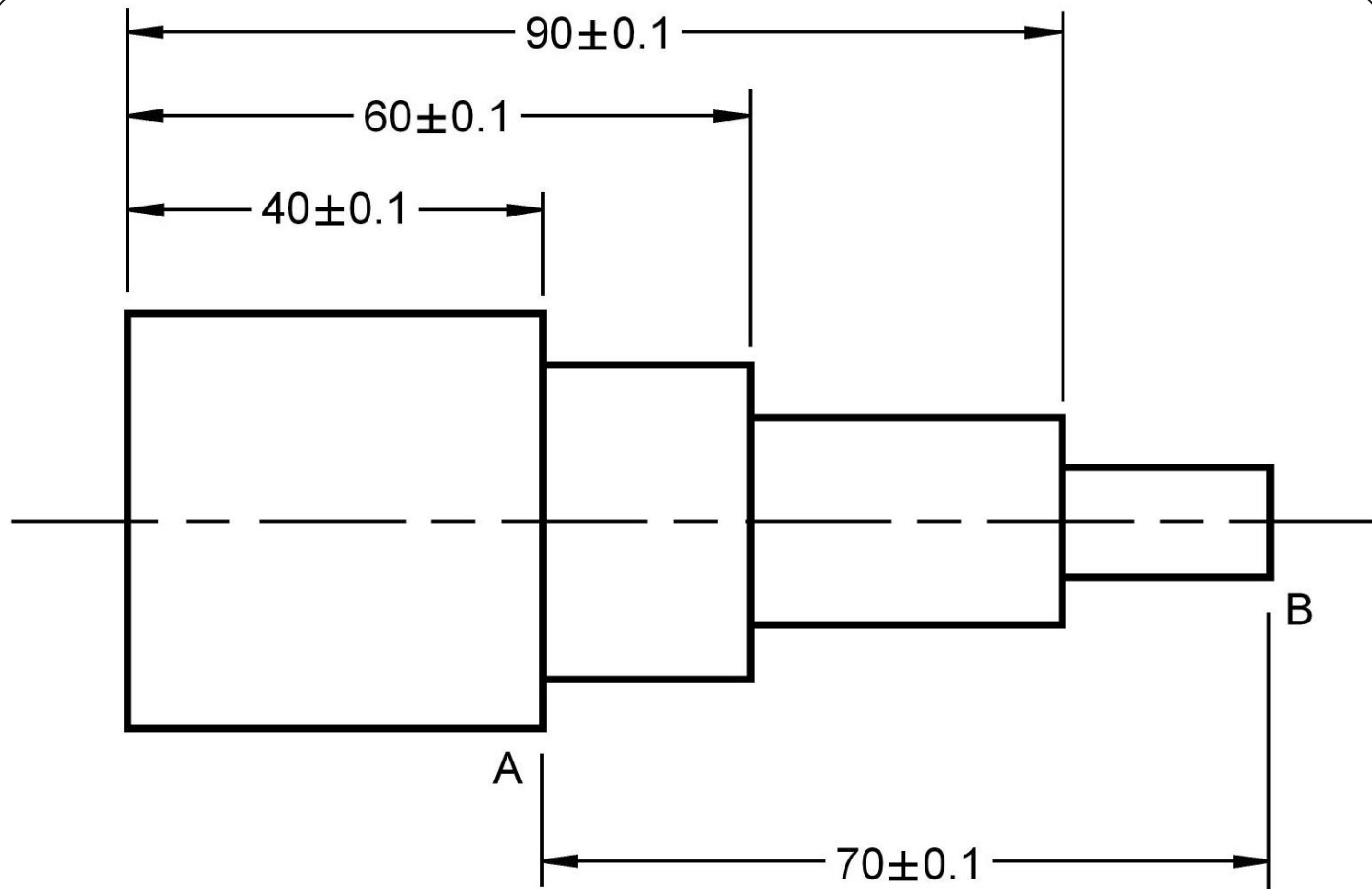
# Tolerance Accumulation



# Tolerance Accumulation



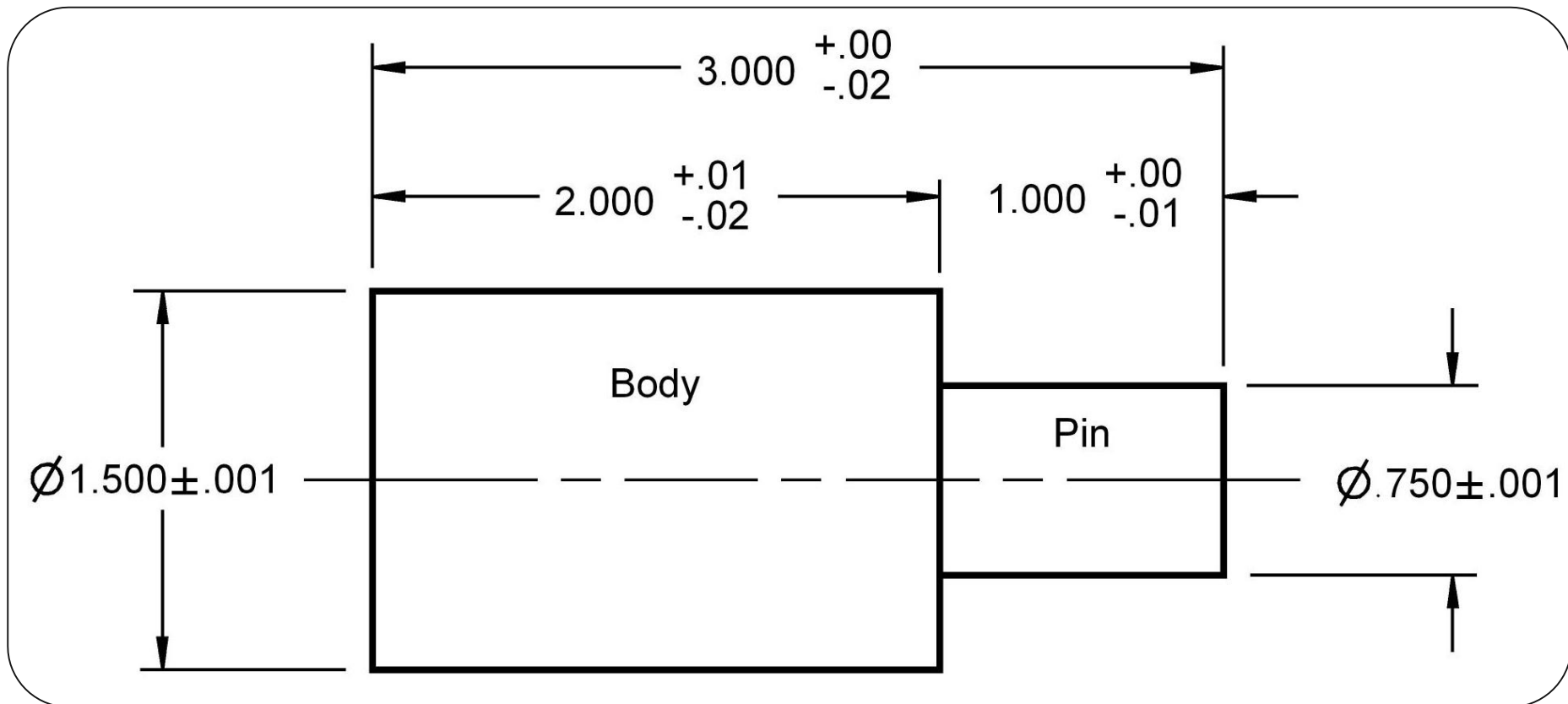
# Tolerance Accumulation



Tolerance accumulation between surface A and B = **0.1**

# Example 17

- Assuming that the diameter dimensions are correct, explain why this object is dimensioned **incorrectly**



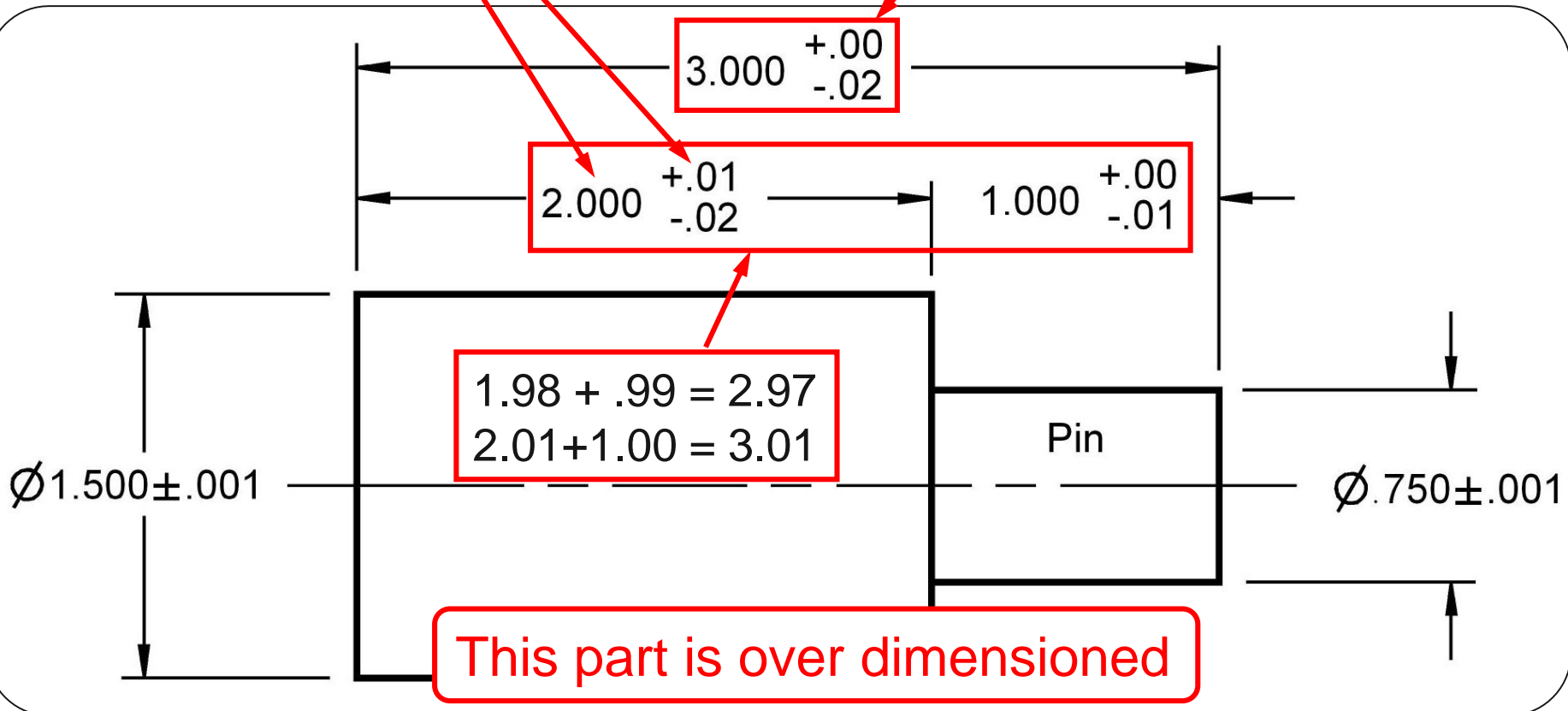


# Example 17

1. The decimal places don't match

2. The dimensions are inconsistent

2.98 – 3.00



This part is over dimensioned

# IX. Formatting Tolerances

# Formatting Metric Tolerances

- Tolerances from standardized fit tables are listed on drawings as:

$\begin{matrix} \phi 20.240 \\ 20.110 \end{matrix} (\phi 20 \text{ C11})$

$\phi 20 \text{ C11} \left( \begin{matrix} \phi 20.240 \\ 20.110 \end{matrix} \right)$

$\phi 20 \text{ C11}$

The person reading the print must have access to the standard fit tables

(K. Plantenberg, 2006,)

# Formatting Metric Tolerances

- **Unilateral tolerances**

$$40 \begin{matrix} 0 \\ -0.02 \end{matrix} \quad \text{or} \quad 40 \begin{matrix} +0.02 \\ 0 \end{matrix}$$

- A single zero without a plus or minus sign

- **Bilateral tolerances**

$$10 \begin{matrix} +0.25 \\ -0.10 \end{matrix} \quad \text{not} \quad 10 \begin{matrix} +0.25 \\ -0.1 \end{matrix}$$

- Both the plus and minus values have the same number of decimal places

# Formatting Metric Tolerances

- **Limit dimensions**

|       |     |                  |
|-------|-----|------------------|
| 15.45 | not | <del>15.45</del> |
| 15.00 |     | <del>15</del>    |

➤ Both values should have the same number of decimal places

- **Using Basic dimensions with the tolerance**

|         |     |                       |
|---------|-----|-----------------------|
| 45±0.15 | not | <del>45.00±0.15</del> |
|---------|-----|-----------------------|

➤ The number of decimal places in the basic dimension does not have to match the number of decimal places in the tolerance

# Formatting Inch Tolerances

- Unilateral and Bilateral tolerances

|   |     |  |
|---|-----|--|
| $.500 \begin{matrix} +.000 \\ -.002 \end{matrix}$ | not | <del><math>.500 \begin{matrix} 0 \\ -.002 \end{matrix}</math></del>    |
| $.500 \begin{matrix} +.001 \\ -.002 \end{matrix}$ | not | <del><math>.50 \begin{matrix} +.001 \\ -.002 \end{matrix}</math></del> |

- The basic dimension and the plus and minus values should have the same number of decimal places

# Formatting Inch Tolerances

- **Limit dimensions**

|              |     |                        |
|--------------|-----|------------------------|
| .250<br>.252 | not | <del>.25<br/>252</del> |
|--------------|-----|------------------------|

➤ Both values should have the same number of decimal places

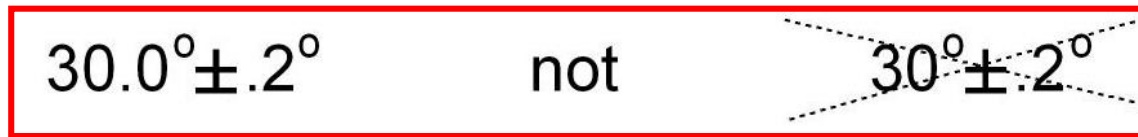
- **Using Basic dimensions with the tolerance**

|             |     |                      |
|-------------|-----|----------------------|
| 2.000±0.015 | not | <del>2.0±0.015</del> |
|-------------|-----|----------------------|

➤ The number of decimal places in the basic dimension should match the number of decimal places in the tolerance

# Formatting Angular Tolerances

- Angular tolerances



- Both the angle and the plus and minus values have the same number of decimal places

(K. Plantenberg , 2006, )



# Summary 1/2

- **Tolerance** is the difference between two limits
- If a feature's size is toleranced , it is allowed to **vary within a range of values or limits**
- **Tolerancing** enables an engineer to **design interchangeable** or **replacement parts**
- **Allowance** is the **difference between the largest shaft diameter** and the **smallest hole diameter**
- The two most common standards agencies are; **American National Standards Institute (ANSI) / (ASME)** and **International Standards Organization (ISO)**

# Summary 2/2

- **The International Tolerance Grade number (IT#) is set of tolerances that vary according to the basic size and provide the same relative level of accuracy within a given grade 00**

# References

1. Dimensioning and Tolerancing, Engineering Drawing and Related Documentation Practices ,ASME Y14.5-2009
2. Engineering Graphics Essentials With AutoCAD 2007, K. Plantenberg
3. Manufacturing, Engineering & Technology, Fifth Edition, by S. Kalpakjian and S. R. Schmid
4. Tolerancing Topics - Exercises presentation ,2006, K.Plantenberg
5. Φυλλάδιο εργαστηριακών ασκήσεων Μηχανουργείου,2012.Δημητρακόπουλος Γ., Μούρτζης Δ., Πανδρεμένος Ι., Παπακώστας Ν., Σταυρόπουλος Π., Φυσικόπουλος Α.